

Article

PROBABILISTIC ACTUAL CAUSATION

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Abstract: Actual (token) causation – the sort of causal relation asserted to hold by claims like *the Chicxulub impact caused the Cretaceous-Paleogene extinction event*, *Mr. Fairchild's exposure to asbestos caused him to suffer mesothelioma*, and *the H7N9 virus outbreak was caused by poultry farmers becoming simultaneously infected by bird and human 'flu strains* – is of significance to scientists, historians, and tort and criminal lawyers. Progress has been made in explicating the actual causal relation in the deterministic case by means of the use of structural equations models and causal graphs. I seek to make similar progress concerning the probabilistic case by using probabilistic causal models and associated causal graphs.

Keywords: probabilistic actual causation; probabilistic causal models; causal graphs

1. Introduction

Actual (token) causation is the sort of causal relation asserted to hold by claims like *the Chicxulub impact caused the Cretaceous-Paleogene extinction event*, *Mr. Fairchild's exposure to asbestos caused him to suffer mesothelioma*,¹ and *the H7N9 virus outbreak was caused by poultry farmers becoming simultaneously infected by bird and human 'flu strains*. Claims about actual causation contrast with generic (type) causal claims, such as *asteroid impacts cause extinction events* and *asbestos exposure causes mesothelioma*. There is little consensus on the relation between actual and generic causation,² but my subject matter is actual causation which can be and has been fruitfully theorised about in its own right (classic theories include those of 2, 3, 4, and 5). Actual causation is of significance to scientists, to historians, and to tort and criminal lawyers.

Since the turn of the millennium – and prompted in particular by a hugely influential book written by the computer scientist, Judea Pearl [6] – the formal tools of Structural Equation Models (SEMs) have started to be brought to bear in attempting to provide a clearer understanding of actual causation.³ SEMs allow for the perspicuous representation of complex patterns of dependence between variables, facilitating the identification of various types of causal structure. This has led to the development of a number of sophisticated accounts of actual causation, enhancing our understanding of that relation.

One limitation of existing accounts, however, is that they mostly focus on the phenomenon of deterministic actual causation (cf. 9, p. 852; 11, p. 498). Roughly speaking, this is the case where the set of all of an event's actual causes suffice for its occurrence. Yet determinism is at best a special case (or even an idealization). According to the orthodox interpretation of quantum mechanics (and several heterodox interpretations), our universe is a non-deterministic, probabilistic one. Moreover, it's not just

¹ *Fairchild v Glenhaven Funeral Services Ltd* ([2002] UKHL 22; [2003] 1 AC 32).

² My preferred view is that actual causation is the fundamental causal relation, and that generic causal claims simply (generically) quantify over actual causal relations [1].

³ Such an approach is taken in, for example, [6], [7], [8], [9], [10], [11], [12], [13], [14], [15], [16], [17], and [18].

31 in fundamental physics that probabilities figure. They also figure heavily in the higher-level sciences,
 32 such as statistical mechanics, genetics, ecology, meteorology, and economics. It is thus a significant
 33 limitation of a theory of actual causation if it doesn't apply to cases of probabilistic causation, such as
 34 an atom's being caused to decay by alpha bombardment, or a person's suffering mesothelioma as a
 35 result of asbestos exposure.⁴

36 In this paper, I will seek to go some way toward addressing this lacuna in a way that builds
 37 upon the successes of SEM approaches to deterministic actual causation. Specifically, I will employ
 38 the formal tools of probabilistic causal models – probabilistic analogues of deterministic SEMs – and
 39 associated causal graphs to provide an analysis of actual causation that is adequate to the probabilistic
 40 case.

41 2. Probability-Raising

42 *Probability-raising* is central to the account developed here – as it is on traditional accounts of
 43 probabilistic actual causation.⁵ To explain how I will understand that notion a bit of stage-setting is
 44 required.

45 Following those who have sought to analyse deterministic actual causation by appeal to SEMs, I
 46 take the relata of the actual causal relation to be variable values. Adopting Goldszmidt and Pearl's
 47 [26, pp. 669-70] notation, $P(W = w|do(V = v))$ represents the probability of the variable W taking the
 48 value $W = w$ that *would* obtain if the variable V were set to the value $V = v$ by an 'intervention' [12, p.
 49 98].⁶ This is liable to diverge from the conditional probability $P(W = w|V = v)$: witness the difference
 50 between the probability of a storm *conditional* upon the barometer needle pointing toward the word
 51 'storm' and the probability of a storm if I had intervened upon the barometer needle to point it toward
 52 'storm'.

53 I shall take it that variable X taking the value $X = x$ rather than $X = x'$ raises the probability of
 54 variable Y taking the value $Y = y$ in the relevant sense iff:⁷

$$P(Y = y|do(X = x)) > P(Y = y|do(X = x')). \quad (1)$$

55
 56 Defining probability-raising in this way – rather than via simple conditional probabilities – means
 57 avoiding probability-raising relations between independent effects of a common cause, such as the
 58 barometer reading and the storm.

59 The above definition defines a three-place, contrastive, relation of probability-raising: ' X taking
 60 the value $X = x$ rather than $X = x'$ raises the probability of $Y = y$ '. I take both actual causation and
 61 probability-raising to be inherently contrastive.⁸ For instance, one might ask: did the driver's driving
 62 at 60mph cause the crash? Relatedly: did the driver's driving at 60mph raise the probability of the
 63 crash? I suspect the former question is virtually unanswerable. The latter may be answerable, but only
 64 if we have a well defined probability distribution over all the possible speeds the driver might have
 65 travelled. More tractable, and perfectly cogent, questions are: did the driver's driving at 60mph rather

⁴ The latter depends not only upon the statistical mechanical processes of diffusion, but also (it is believed) upon the molecular bonding processes involved in, for example, the stimulation of macrophages by the HMGB1 protein. These bonding processes are subject to quantum probabilities.

⁵ See, for example, [19], [20], [21, p. 204], [22], [23, pp. 175-84], [5]. The deficiencies of these accounts have been demonstrated in e.g. [4, pp. 192-202]; [24, pp. 85-96], and [25].

⁶ The notion of an 'intervention' is itself a causal notion. Still, I follow Woodward [12, pp. 20-2, 104-7] in thinking that an account of causation can be illuminating even if not reductive. If one wishes to pursue a reductive account, then it's worth noting that the Lewisian semantics for counterfactuals Lewis [27] – which does not appeal to causal notions – can be extended to cover the sort of counterfactual appealed to in the present paper (see [28]).

⁷ Here and throughout, the probabilities should be taken to be those obtaining immediately after all of the interventions bringing about the variable values specified in the scope of the $do(\cdot)$ function have occurred [cf. 23, p. 177].

⁸ On the contrastivity of actual causation, see [29], [30], [31], [32], and [9, p. 859].

66 than less than 60mph (alternatively: rather than more than 60mph; or: rather than below the 40mph
 67 speed limit) cause the crash? Did the driver's driving at 60mph rather than less than 60mph raise
 68 the probability of the crash? The latter questions have two features: (i) they wear their contrastivity
 69 on their face; (ii) the contrast is with an alternative relative to which it is (presumably) clear that the
 70 driver's driving at 60mph is a probability-raiser and cause of the crash. The former questions were
 71 not explicitly contrastive and I take it that the default contrast where no contrast is explicitly stated or
 72 made salient by context is that it is simply the complement of the event in question (in this case the
 73 driver's driving at 60mph). This is why the questions were difficult to answer: some of the possibilities
 74 contained in the complement of the driver's driving at 60mph are possibilities in which she drove at
 75 greater than 60mph (and so, presumably, the probability of a crash was still higher) while some of
 76 them are possibilities in which she drove at less than 60mph (and so, presumably, the probability of a
 77 crash was lower).

78 Both the formal definition of probability-raising above and the definition of actual causation
 79 below are explicitly contrastive. However, since most of the examples that I will discuss can be
 80 represented using just sets of binary variables, I shall often suppress mention of the contrast in my
 81 informal discussion since it will be obvious that the contrast is just with the only alternative value of
 82 the variable in question.⁹

83 The key problems confronting attempts to analyze probabilistic actual causation – and an informal
 84 statement of the solutions that I propose – can be introduced by means of a series of examples, which I
 85 describe in the following section.

86 3. Problem Cases

87 3.1. Fizzling

88 The first example is a case of what Schaffer [33, p. 81] calls 'fizzling'.¹⁰ Such cases show that
 89 probability-raising – even when understood in the interventionist sense given in the previous section

⁹ The definitions offered here analyze three-place relations, taking the form 'Variable X taking the value $X = x$ rather than $X = x'$ raised the probability/was an actual cause of variable Y 's taking the value $Y = y$ iff ...'. But should we in fact take probability-raising and/or actual causation to be a four place relation? Briefly: probability-raising is (as indicated in the main text) naturally taken as a three-place relation, but not as a four-place relation: I don't think 'Variable X taking the value $X = x$ rather than $X = x'$ raised the probability of variable Y taking the value $Y = y$ rather than $Y = y'$ ' has a clear interpretation. It is more plausible that actual causation should be treated as a four-place relation (cf. [31, p. 328], [12, p. 146]): for example, claims like 'Doctor's administering 20mg rather than 10mg of Drug to Patient caused Patient to recover quickly rather than slowly' seem coherent. A first pass at an analysis of a quaternary relation of actual causation would be: 'Variable X taking the value $X = x$ rather than $X = x'$ was an actual cause of variable Y taking the value $Y = y$ rather than $Y = y'$ iff (i) $P(Y = y|do(X = x)) > P(Y = y|do(X = x'))$ and (ii) $P(Y = y'|do(X = x')) > P(Y = y'|do(X = x))$ (e.g. Doctor's administering 20mg rather than 10mg raised the probability of Patient's recovering quickly but Doctor's administering 10mg rather than 20mg would have raised the probability of Patient's recovering slowly). Though I shall not discuss this in detail here, my proposed final analysis of a four-place actual causal relation (in light of the concepts that will be introduced below) would be that variable X taking the value $X = x$ rather than $X = x'$ was an actual cause of variable Y taking the value $Y = y$ rather than $Y = y'$ iff relative to at least one apt model, variable X taking the value $X = x$ rather than $X = x'$ is an unneutralized de facto probability-raiser of variable Y taking the value $Y = y$, while variable X 's taking the value $X = x'$ rather than $X = x$ is a de facto probability-raiser of $Y = y'$. Where X and Y are binary variables (as is the case with most of the examples of putative cause and effect variables to be discussed below), it is automatically the case that $X = x'$ (de facto) raises the probability of $Y = y'$ if $X = x$ (de facto) raises the probability of $Y = y$, so we won't need to explicitly take note of this additional complication.

¹⁰ In illustrating each of the causal structures discussed in this section, I will use a vignette that is a variant on one given in [34] (cf. [35, p. 147] and [36, p. 176]), where it is used to illustrate the general phenomenon of probabilistic actual causation. I have deliberately chosen vignettes in which the probabilities involved are quantum, to minimize the scope for dispute over whether they are the sort of objective chances that are apt to underwrite objective actual causal relations. (It is true that the probabilities assigned to agents' making decisions in these examples are not quantum probabilities. But if you're worried that they're therefore not objective, the example could be complicated so that the various 'actions' described depend on the outcomes of quantum measurements rather than ordinary decisions.) In fact, I'm sympathetic to the view that there are objective chances that aren't simply quantum probabilities. (On this latter point, see [37], [38], [39], [40], [41], [42], and [43], *inter alia*).

90 so as to rule out ‘spurious’ probability raising between independent effects of a common cause – is not
91 sufficient for causation.

Fizzling

Someone has hooked up a nuclear bomb to a detonator. The detonator is wired to a Geiger counter so that, if the Geiger counter registers above a threshold reading, then the bomb will (with probability ≈ 1) be detonated. I have some Uranium-232 and I place this near to the Geiger counter. The threshold for activating the detonator is such that, given the probabilistic nature of U-232 decay, there’s a probability 0.8 that the Geiger counter will register above the threshold.

If I’d refrained from placing the U-232 near to the Geiger counter, then there would have been a 0.00001 chance of the bomb exploding. This is because the bomb is a nuclear device with a Uranium-235 core and there’s a certain (very small) probability that enough U-235 atoms in the bomb undergo spontaneous α -decay to start a chain reaction resulting in the bomb’s (spontaneously) exploding.

In fact, the threshold reading of the Geiger counter isn’t reached, but the bomb nevertheless explodes.

92 In **Fizzling**, my placing the U-232 near to the Geiger counter was not an actual cause of the bomb’s
93 exploding. Rather, the bomb’s exploding is a consequence of spontaneous U-235 decay in its core. As
94 a matter of probability, the probabilistic process by which my action threatened to bring about the
95 bomb’s explosion ‘fizzled out’ – as a result of the Geiger threshold not being reached – before it could
96 bring about the explosion.

97 Suppose that M is a binary variable that takes value $M = 1$ if I place the U-232 near to the Geiger
98 counter and $M = 0$ if I don’t. And suppose that E is a binary variable that takes value $E = 1$ if the
99 bomb explodes and $E = 0$ if it does not. Then my action raises the probability of the bomb’s exploding
100 in the sense that:

$$P(E = 1|do(M = 1)) = 0.8 > 0.00001 = P(E = 1|do(M = 0)). \quad (2)$$

101 The example thus shows that probability-raising is not sufficient for actual causation.

102 Let me briefly anticipate the approach that I shall take below in tackling the problem posed by
103 **Fizzling**. In my view, the probabilistic fact that leads us to consider my action not to be an actual cause
104 of the bomb’s exploding in this case is the fact that *the probability of the bomb’s exploding given that I*
105 *placed the U-232 near to the Geiger counter but the Geiger counter did not register above the threshold reading*
106 *is no higher than the probability of the bomb’s exploding would have been if I’d never placed the U-232 near to*
107 *the Geiger counter in the first place.*

108 Where T is a binary variable that takes $T = 1$ if the threshold reading is reached and $T = 0$ if it
109 isn’t, then this probabilistic fact is expressed formally as follows:

$$P(E = 1|do(M = 1 \& T = 0)) \leq P(E = 1|do(M = 0)). \quad (3)$$

110 Indeed the terms on the left- and right-hand side of the above inequality are both equal to 0.00001.

111 In light of the obtaining of the above inequality, we might say that the probability-raising of
112 $E = 1$ by $M = 1$ is ‘neutralized’ by the fizzling event represented by $T = 0$. This sort of probabilistic
113 ‘neutralization’ will play an important role in the analysis of probabilistic actual causation to be
114 developed below.

115 3.2. Probabilistic Preemption

116 In the previous section we considered an example that shows that probability-raising is not sufficient
117 for actual causation. A second example – a case of probabilistic preemption – illustrates that
118 probability-raising is not necessary either.

Probabilistic Preemption

Someone (neither you nor I) has connected a Geiger counter to a bomb so that the bomb will explode if the Geiger counter registers above a threshold reading. I place a chunk of U-232, which has a half-life of 68.9 years and decays by α -emission, near to the Geiger counter. By chance, enough U-232 atoms decay within a short enough interval for the Geiger counter to reach the threshold reading so that the bomb explodes.

Unbeknownst to me, you've been standing nearby observing. You have a chunk of Th-228, which has a half-life of 1.9 years and decays by α -emission, which contains at least as many atoms as my chunk of U-232. You've decided that you'll place your Th-228 near to the Geiger counter iff I fail to place my U-232 near to the Geiger counter. There's a negligible chance that you won't follow the course of action that you've decided upon. Seeing that I place my U-232 near to the Geiger counter, you don't place your Th-228 near to the Geiger counter.

(The range of α -particles is 3-5 cm. Suppose – here and in the following examples – that, for each of us, to place our chunk 'near' to the Geiger counter is to place it ≤ 5 cm away. There is a slight complication if the chance of an alpha particle travelling more than 5cm is not zero, but merely very small, especially if there's a non-zero probability of an alpha particle travelling from wherever your Th-228 is in fact located when you decide not to place it near to the Geiger counter. If there is, then we need to augment the story with the stipulation that no alpha particle traverses the region of space between your Th-228 and the Geiger counter sensor during the relevant interval if we are to conclude that alpha emission from your Th-228 was not an actual cause. If some of the alpha particles that reached the sensor during the relevant interval did in fact come from your Th-228, and some came from my U-232, then I would take alpha emission from each to be a cause of the bomb's exploding. But for the purposes of the present example, we'll assume that no alpha particles from your Th-228 make it.)

119 In this case, my placing my U-232 near the Geiger counter is plausibly regarded as an actual cause of
 120 the bomb's exploding. Let M , D , Y , T , and E be binary variables which, respectively, take value 1 if
 121 the following things occur (and 0 otherwise): I place my U-232 near to the Geiger counter; you decide
 122 to place your Th-228 near to the Geiger counter iff I don't place my U-232 near to the Geiger counter;
 123 you place your Th-228 near to the Geiger counter; the threshold Geiger counter reading is reached; the
 124 bomb explodes.

125 Though my act ($M = 1$) was an actual cause of the explosion ($E = 1$), the following inequality
 126 holds:

$$P(E = 1|do(M = 1)) < P(E = 1|do(M = 0)). \quad (4)$$

127 That is, my placing my U-232 near to the Geiger *lowers* the probability of the bomb's exploding. That's
 128 because it strongly lowers the probability of your placing your more potent Th-228 near to the Geiger
 129 (your Th-228 is more potent because Th-228 has a shorter half life than U-232 and your chunk of Th-228
 130 contains at least as many atoms as my chunk of U-232). Probability-raising is therefore unnecessary for
 131 actual causation.

132 Let me briefly anticipate the approach I shall take in tackling the problem posed by **Probabilistic**
 133 **Preemption** below. In my view, the probabilistic fact that inclines us to consider my action to be an
 134 actual cause of the bomb's explosion is the fact that *holding fixed your failure to place your Th-228 near to the Geiger counter, my placing my U-232 near to the Geiger raises the probability of the bomb's exploding*.¹¹
 135 Formally:
 136

$$P(E = 1|do(M = 1 \& Y = 0)) > P(E = 1|do(M = 0 \& Y = 0)). \quad (5)$$

¹¹ Similar views are articulated in [44], [45], and [46].

137 The idea is that, although my action doesn't straightforwardly raise the probability of the bomb's
 138 exploding (because it lowers the probability of your placing your Th-228 near to the Geiger counter),
 139 my action does raise the probability of the bomb's exploding *when we hold fixed the background fact that*
 140 *you don't place your Th-228 near to the Geiger counter*. This is a probabilistic analogue of what, in the
 141 deterministic case, Stephen Yablo ([47], [48]) has called *de facto dependence*: the latter comprising latent
 142 counterfactual dependence that is revealed when certain background facts about the actual world are
 143 held fixed. In this context, we might call it *de facto probability-raising*.¹²

144 The analysis of probabilistic actual causation that will be developed below will incorporate the
 145 idea that it is this sort of *de facto* probability-raising, rather than straightforward probability-raising
 146 that is a necessary condition for causation.

147 3.3. Fizzled Preemption

148 Is *de facto* probability-raising – that is, probability-raising *holding appropriate background factors fixed* –
 149 sufficient for actual causation? Unfortunately, the answer is 'no', as can be seen from the following
 150 example, which is a sort of hybrid of the previous two.

Fizzled Preemption

Someone has connected a Geiger counter to a bomb so that the bomb will explode if the Geiger counter registers above a threshold reading. I place a chunk of U-232 near to the Geiger counter. Unbeknownst to me, you've been standing nearby observing. You have a chunk of Th-228, which contains at least as many atoms as my chunk of U-232. You've decided that you'll place your Th-228 near to the Geiger counter iff I fail to place my U-232 near to the Geiger counter. There's a negligible chance that you won't follow the course of action that you've decided on. Seeing that I place my U-232 near to the Geiger counter, you don't place your Th-228 near to the Geiger counter. The threshold reading of the Geiger counter isn't reached, but the bomb nevertheless explodes (there was a very small background chance of enough atoms in its U-235 core spontaneously decaying to start a chain reaction resulting in the bomb's exploding).

151 This time, my act was not an actual cause of the bomb's exploding because the threshold reading
 152 of the Geiger counter was not reached. Nevertheless, exactly the same inequality obtains as in the
 153 **Probabilistic Preemption** case, namely:

$$P(E = 1 | do(M = 1 \& Y = 0)) > P(E = 1 | do(M = 0 \& Y = 0)) \quad (6)$$

154 This illustrates that *de facto* probability-raising is not sufficient for causation.

155 Just as in **Fizzling**, the probabilistic process via which my action threatens to bring about the
 156 explosion is fizzled by the Geiger counter's not reaching the relevant threshold. I suggest that the
 157 probabilistic fact that corresponds to the intuition that my action is not an actual cause of the bomb's
 158 exploding in this case is that *even holding fixed your (in)action, the probability of the bomb's exploding given*
 159 *my placing my U-232 near to the Geiger counter but the threshold's not being reached is no higher than the*
 160 *probability of the explosion if I had never placed my U-232 near to the Geiger in the first place*. Formally:

$$P(E = 1 | do(M = 1 \& T = 0 \& Y = 0)) \leq P(E = 1 | do(M = 0 \& Y = 0)) \quad (7)$$

161 In other words, just as straightforward probability-raising can be neutralized by a fizzling event, so
 162 too can *de facto* probability-raising (which, in light of **Probabilistic Preemption**, is a more plausible
 163 *necessary* condition for actual causation than is straightforward probability-raising).

¹² One of the challenges to be addressed below is to specify *which* background factors are the appropriate ones to hold fixed.

164 The upshot is a simple proposal: *probabilistic actual causation is to be identified with unneutralized*
 165 *de facto probability-raising*. It is this proposal that I shall seek to develop in the remainder of the paper.
 166 Making the proposal precise will involve a certain amount of stage setting, to be done in the next
 167 section.

168 Before proceeding, it is worth making an observation about the examples introduced so
 169 far. This is that, although **Fizzled Preemption** was introduced to make vivid the fact that
 170 de facto probability-raising is not sufficient for causation – due to the possibility of its being
 171 neutralized –, **Fizzling** and **Probabilistic Preemption** also illustrate this fact. **Fizzling** illustrates
 172 it because straightforward probability-raising can be considered to be just a limiting case of de facto
 173 probability-raising: it is probability-raising holding the null event fixed. And, in **Fizzling**, although
 174 $M = 1$ raised the probability of $E = 1$ holding the null event fixed as per Inequality (2), $M = 1$ was not
 175 an actual cause of $E = 1$ because this de facto probability-raising is neutralized as per Inequality (3).

176 **Probabilistic Preemption** also illustrates the fact that de facto probability-raising isn't sufficient
 177 for actual causation. For, although in **Probabilistic Preemption** my action de facto raises the probability
 178 of the explosion *and* is an actual cause of it, your decision ($D = 1$) to place your Th-228 near to the
 179 Geiger counter iff I don't also de facto raises the probability of the explosion,¹³ even though it is *not* an
 180 actual cause of the explosion since you don't place your Th-228 near to the Geiger counter. Indeed,
 181 plausibly, your decision straightforwardly raised the probability of the bomb's exploding. That is:

$$P(E = 1|do(D = 1)) > P(E = 1|do(D = 0)) \quad (8)$$

182

183 Inequality (8) holds provided there's some chance that $M = 0$, because $D = 1$ raises the probability
 184 that the bomb will still explode in the scenario in which $M = 0$.¹⁴ Nevertheless, as we'll see below, this
 185 de facto probability-raising (holding the null event fixed) is neutralized by the fact that you in fact
 186 don't place your Th-228 near to the Geiger counter.

187 4. Probabilistic Causal Models

188 In order to render more precise the idea that actual causation might be identified with unneutralized
 189 de facto probability-raising, it is helpful to make use of Probabilistic Causal Models (PCMs). A PCM,
 190 \mathcal{M} , is a 6-tuple $\langle \mathcal{V}, \mathcal{R}, \mathcal{C}, \Omega, \mathcal{F}, do(\cdot) \rangle$. Here \mathcal{V} is a set of variables. \mathcal{R} is a function from elements of \mathcal{V} to
 191 sets of values: for all $V_i \in \mathcal{V}$, $\mathcal{R}(V_i)$ is the *range* of V_i . In Halpern and Pearl's [9, pp. 851-2] terminology,
 192 a formula $V_i = v_i$, for $V_i \in \mathcal{V}$ and $v_i \in \mathcal{R}(V_i)$, is a *primitive event*. \mathcal{C} is the set of all those possible
 193 conjunctions of primitive events, $V_1 = v_1 \& \dots \& V_n = v_n$, such that $V_i \in \mathcal{V}$ and $v_i \in \mathcal{R}(V_i)$ and such
 194 that, for no pair of conjuncts $V_i = v_i, V_j = v_j$ is $V_i \equiv V_j$, and where no two elements of \mathcal{C} differ *only* in
 195 the permutation of their conjuncts. Such a conjunction is denoted $\mathbf{V} = \mathbf{v}$ (primitive events and the
 196 null event are limiting cases of such conjunctions). Abusing notation, the fact that $v_i \in \mathcal{R}(V_i)$ for each
 197 primitive event $V_i = v_i$ in the conjunction $\mathbf{V} = \mathbf{v}$, is abbreviated $\mathbf{v} \in \mathcal{R}(\mathbf{V})$ and the set of variables that
 198 appear in $\mathbf{V} = \mathbf{v}$ is denoted \mathbf{V} .

199 Call a conjunction $\mathbf{V} = \mathbf{v}$ *maximal* iff it contains a conjunct of the form $V_i = v_i$ for each $V_i \in \mathcal{V}$.
 200 Ω is the set of all maximal conjunctions of primitive events. \mathcal{F} is a sigma algebra on Ω . Finally,
 201 $do(\cdot)$ is a function from elements of \mathcal{C} to probability distributions on \mathcal{F} [cf. 7, pp. 70, 110]: for each
 202 element $\mathbf{V} = \mathbf{v}$ of \mathcal{C} , $P(\cdot|do(\mathbf{V} = \mathbf{v}))$ is the probability (chance) distribution on \mathcal{F} that *would* obtain if
 203 interventions were performed to bring about $\mathbf{V} = \mathbf{v}$.

¹³ At least if we assume that the most probable alternative is for you to decide not to place your Th-228 near to the Geiger counter come what may.

¹⁴ That probabilistic preemption cases illustrate both that straightforward probability-raising (i.e. probability-raising under the null contingency) is neither necessary nor sufficient for actual causation was first observed by Menzies ([5], [24]).

204 The graph \mathcal{G} associated with a PCM, $\mathcal{M} = \langle \mathcal{V}, \mathcal{R}, \mathcal{C}, \Omega, \mathcal{F}, do(\cdot) \rangle$, is an ordered pair $\langle \mathcal{N}, \mathcal{E} \rangle$ such
 205 that \mathcal{N} is a set of nodes and \mathcal{E} is a set of directed edges or ordered pairs of nodes, with $\mathcal{N} \equiv \mathcal{V}$ and
 206 $\langle V_i, V_j \rangle \in \mathcal{E}$ iff, where $\mathbf{S} = \mathcal{V} \setminus V_i, V_j$, there is some assignment of values $\mathbf{s}' \in \mathcal{R}(\mathbf{S})$, some pair of values
 207 $v_i, v'_i \in \mathcal{R}(V_i)$ ($v_i \neq v'_i$) and some value $v_j \in \mathcal{R}(V_j)$ such that $P(V_j = v_j | do(V_i = v_i; \mathbf{S} = \mathbf{s}')) \neq P(V_j =$
 208 $v_j | do(V_i = v'_i; \mathbf{S} = \mathbf{s}'))$. The graph \mathcal{G} can be represented diagrammatically by taking the elements of
 209 \mathcal{N} as vertices and drawing an arrow from V_i to V_j iff $\langle V_i, V_j \rangle \in \mathcal{E}$.

210 To construct a PCM, \mathcal{M}_{Fiz} , of **Fizzling**, we might take the variable set \mathcal{V}_{Fiz} to be $\{M, T, E\}$. The
 211 range of each variable in \mathcal{V}_{Fiz} is the pair $\{0, 1\}$. \mathcal{C}_{Fiz} , Ω_{Fiz} , and \mathcal{F}_{Fiz} are generated by \mathcal{V}_{Fiz} and \mathcal{R}_{Fiz} in
 212 the way described above. For each element of \mathcal{C}_{Fiz} , the function $do(\cdot)$ returns the chance distribution
 213 on \mathcal{F}_{Fiz} that would obtain if interventions were performed to bring about that element of \mathcal{C}_{Fiz} . The
 214 graph for \mathcal{M}_{Fiz} is given as Figure 1.



Figure 1

215 We can also construct a PCM, $\mathcal{M}_{\text{ProbPre}}$, of **Probabilistic Preemption**. In doing so, we might take
 216 the variable set to be $\mathcal{V}_{\text{ProbPre}} = \{D, M, Y, T, E\}$. The range of each variable in $\mathcal{V}_{\text{ProbPre}}$ is the pair
 217 $\{0, 1\}$. $\mathcal{C}_{\text{ProbPre}}$, Ω_{ProbPre} , and $\mathcal{F}_{\text{ProbPre}}$ are generated by $\mathcal{V}_{\text{ProbPre}}$ and $\mathcal{R}_{\text{ProbPre}}$ in the way described
 218 above. For each element of $\mathcal{C}_{\text{ProbPre}}$, the function $do(\cdot)$ returns the chance distribution on $\mathcal{F}_{\text{ProbPre}}$ that
 219 would obtain if interventions were performed to bring about that element of $\mathcal{C}_{\text{ProbPre}}$. The graph for
 220 $\mathcal{M}_{\text{ProbPre}}$ is given as Figure 2.

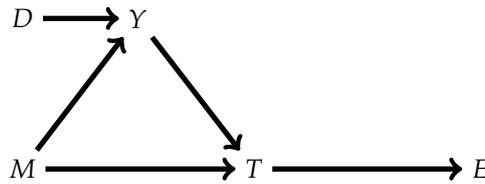


Figure 2

221 A further piece of terminology will be useful in what follows: a *directed path* in a graph is an ordered
 222 sequence of nodes, $\langle V_1, V_2, \dots, V_n \rangle$, such that there is a directed edge from V_1 to V_2 , and a directed
 223 edge from V_2 to $\dots V_n$. $\langle M, Y, T, E \rangle$ is an example of a directed path in the graph of $\mathcal{M}_{\text{ProbPre}}$.

224 It is worth noting that $\mathcal{M}_{\text{ProbPre}}$ serves just as well as a PCM for **Fizzled Preemption** as it does for
 225 **Probabilistic Preemption**. That's because there is no structural difference between the two examples.
 226 The difference resides only in the fact that in **Fizzled Preemption**, as a matter of probability, the
 227 variable T takes the value $T = 0$ rather than $T = 1$.

228 In Section 6, I will seek to make precise the idea that actual causation can be identified with
 229 unneutralized de facto probability-raising by appealing to PCMs. My specific strategy will be to define
 230 a precise notion of unneutralized de facto probability-raising *relative to a PCM*. I will then provide a
 231 definition of what it is for $X = x$ (rather than $X = x'$) to count as an actual cause of $Y = y$ *relative to*
 232 *a PCM*: namely this is for $X = x$ (rather than $X = x'$) to bear the relation of unneutralized de facto
 233 probability-raising to $Y = y$ *relative to that PCM*. I then define a non-model-relativized notion of actual
 234 causation by saying that $X = x$ (rather than $X = x'$) counts as an actual cause of $Y = y$ *simpliciter*
 235 provided that $X = x$ (rather than $X = x'$) counts as an actual cause of $Y = y$ relative to at least one
 236 *appropriate* PCM. Those who seek to analyze deterministic actual causation in terms of SEMs often
 237 adopt a similar strategy of first defining model-relative (deterministic) actual causation, and then
 238 defining (deterministic) actual causation *simpliciter* in terms of (deterministic) actual causation relative
 239 to at least one appropriate SEM (see, e.g. [10, p. 287], [11, p. 503], [18]).

240 My strategy requires an account of ‘appropriate’ models. Such an account is provided in the next
241 section.

242 5. Appropriate Models

243 Many of the criteria for an appropriate SEM for evaluating deterministic actual causation that have
244 been advanced in the literature carry over to PCMs, including the following three:

245 (Partition) For all $V_i \in \mathcal{V}$, the elements of $\mathcal{R}(V_i)$ should form a partition (16, pp. 397-8; 49, p. 182)

246 (Independence) For no two variables $V_i, V_j \in \mathcal{V}$ ($V_i \neq V_j$) should there be elements $v_i \in \mathcal{R}(V_i)$ and
247 $v_j \in \mathcal{R}(V_j)$ such that the states of affairs represented by $V_i = v_i$ and $V_j = v_j$ are
248 logically or metaphysically related (10, p. 287; 16, p. 397)

249 (Naturalness) For all $V_i \in \mathcal{V}$, each value in $\mathcal{R}(V_i)$ should represent reasonably natural and intrinsic
250 states of affairs. (cf. 49, 182)

251 The analysis of actual causation proposed below (like analyses of deterministic actual causation in
252 terms of SEMs) takes all and only values of distinct variables to be potential causal relata. (Partition)
253 insures that we don’t thereby miss actual causal relations because they obtain between the values of a
254 single variable. (Independence) insures that we don’t mistake stronger-than-causal relations for causal
255 relations. (Naturalness) insures that unnatural or non-intrinsic states of affairs do not get counted as
256 causes and effects (justification of this restriction is given in [23, pp. 190, 263]).^{15,16}

257 A further condition that should be imposed is that a PCM is appropriate for evaluating whether
258 $X = x$ is an actual cause of $Y = y$ in world θ only if it satisfies (Veridicality):

259 (Veridicality) For any conjunction $\mathbf{V} = \mathbf{v} \in \mathcal{C}$ taken as an input, the probability distribution
260 $P(\cdot | do(\mathbf{V} = \mathbf{v}))$ yielded as output by the $do(\cdot)$ function of \mathcal{M} should be the objective
261 chance distribution over \mathcal{F} that would $_{\theta}$ result from interventions setting $\mathbf{V} = \mathbf{v}$.
262 (‘Would $_{\theta}$ ’ indicates that what is required is that this counterfactual be true in θ .)

263 The idea behind (Veridicality) is simply that, in order to capture genuine causal relations between the
264 variables in its variable set, a PCM must capture how the chance distribution over those variables
265 would truly change under interventions on subsets of those variables. (Veridicality) is an analogue – for
266 PCMs – of the requirement typically imposed that ‘appropriate’ SEMs encode only true counterfactuals
267 ([10, p. 287], [11, p. 503]).

268 In the literature in which an analysis of (deterministic) actual causation in terms of SEMs is sought,
269 another condition on model appropriateness is typically added:

270 (Serious Possibilities) \mathcal{V} should not be such as to generate elements of Ω that represent possibilities
271 “that we consider to be too remote” (10, p. 287; cf. 12, pp. 86-91, 18).

272 This condition is needed to avoid a variety of counterintuitive results (see, e.g., [10, p. 287]; [12, pp.
273 86-91]), the canvassing of all of which would take us too far afield. Most straightforwardly, it helps
274 avoid the overgeneration of cases of causation by absence. For instance, JFK’s death presumably
275 counterfactually and probabilistically depends upon Paul McCartney’s failure to get in the way of the

¹⁵ The fact that (Naturalness) refers to ‘reasonably’ natural and intrinsic states of affairs introduces a certain amount of vagueness into the account, but this is necessary because demanding perfect naturalness would presumably rule out high-level states of affairs as causes and effects, which would be implausible.

¹⁶ If *absences* are unnatural states of affairs (cf. 23, pp. 189-93), we might replace (Naturalness) with the requirement that each variable have *at most one value* representing such a state of affairs if we wish to allow (as we will in the following) that absences of reasonably natural events should count as causes and effects and that *events* that are causes and effects may be represented by binary variables that have the absence of these events as one of their values.

276 oncoming bullets. But most of us would be reluctant to say that the latter is a cause of the former. This
 277 is because we view McCartney's getting in the way as a non-serious possibility. (Serious Possibilities)
 278 ensures that no appropriate causal model of the events around JFK's death will include a variable
 279 representing whether or not he gets in the way. Consequently no such model will treat his failure to do
 280 so as a potential cause.

281 Adopting (Serious Possibilities) results in a certain amount of vagueness and, perhaps, subjectivity.
 282 A discussion of whether this is problematic would take us too far afield.¹⁷ But certainly it doesn't put
 283 the present account in any worse shape than its deterministic cousins. Moreover, traditional accounts
 284 of actual causation – which don't appeal to causal models – also stand in need of appeal to 'serious
 285 possibilities' [12, pp. 86-8].¹⁸

286 A final requirement – similar to one imposed in the deterministic actual causation/SEM literature
 287 – for a model \mathcal{M} to be an appropriate one for evaluating whether $X = x$ (rather than $X = x'$) is an
 288 actual cause of $Y = y$ *simpliciter* (i.e. not merely a model-relative actual cause) in world θ is:

289 (Stability) There is no model \mathcal{M}^* (satisfying Partition, Independence, Naturalness, Veridicality, and
 290 Serious Possibilities) with a variable set \mathcal{V}^* such that $\mathcal{V}^* \supseteq \mathcal{V}^{fine}$ – where either $\mathcal{V}^{fine} \equiv \mathcal{V}$
 291 or \mathcal{V}^{fine} differs from \mathcal{V} only in that some of the variables in \mathcal{V}^{fine} are fine-grainings of
 292 variables in \mathcal{V} – relative to which $X = x$ (or: the actual value of some fine-graining X^{fine}
 293 of X) rather than $X = x'$ (or: rather than each of the values of some fine-graining X^{fine} of
 294 X that correspond to $X = x'$) is *not* an actual cause of $Y = y$ (or: the actual value of some
 295 fine-graining Y^{fine} of Y). (cf. 16, pp. 394-5; 15; 11, p. 503).

296 A variable V_1 is a 'fine-graining' of a variable V_2 iff the values of V_2 correspond to equivalence classes
 297 of values of V_1 (cf. 50) or, in other words, iff the values of V_1 are realizers of the values of V_2 . Identity
 298 can be taken as a limiting case of realization so that if some of the values of V_1 are, or represent, states
 299 that are identical to (states represented by) values of V_2 , the former can still be said to realize the latter.
 300 Thus a variable that has a value that represents a car's travelling below 50mph and then values that
 301 represent its travelling at 50-60mph, 60-70mph, etc. can be considered a fine-graining of a binary
 302 variable that simply represents whether it travels below 50mph or above 50mph.

303 The idea behind (Stability) is that an appropriate model is a sufficiently rich representation of
 304 causal reality that moving to a richer representation by including additional variables representing
 305 further factors and/or by representing already-represented factors in more detail would not reveal an
 306 apparent actual causal relation to be spurious.¹⁹ This requirement just reflects the obvious fact that we
 307 don't want to make causal judgements on the basis of a model that's too impoverished to accurately
 308 reflect causal reality. The workings of (Stability) shall be demonstrated on several occasions in the
 309 following.

310 The converse requirement – that a negative verdict about actual causation should not be
 311 overturned in a richer model – isn't needed. This is because actual causation (*simpliciter*) will be
 312 defined in terms of actual causation relative to *at least one* appropriate model. A model-relative verdict
 313 that $X = x$ (rather than $X = x'$) is not an actual cause of $Y = y$ thus automatically fails to translate into
 314 a verdict that $X = x$ (rather than $X = x'$) is not an actual cause (*simpliciter*) of $Y = y$ if there's a richer
 315 (and otherwise appropriate) model relative to which $X = x$ (rather than $X = x'$) is an actual cause of
 316 $Y = y$.

¹⁷ But see [12, pp. 86–91] on this question.

¹⁸ If one regards appeal to 'serious possibilities' in an account of actual causation as too problematic, one option would be to simply admit that, e.g., McCartney's failure to get in the way was an actual cause of JFK's death. If so, as Blanchard and Schaffer [49, p. 198] point out, (Serious Possibilities) "may be reinterpreted, not as an aptness constraint on models, but as a descriptive psychological claim about which causal models are most readily available to us when we form our causal judgements."

¹⁹ Note that (Stability) thus renders the notion of an appropriate model relative to the causal claim being evaluated.

317 6. Probabilistic Actual Causation

318 In this Section, I will define actual causation *simpliciter* in terms of actual causation relative to an
 319 appropriate PCM. I will then define model-relative actual causation in terms of a formally precise
 320 notion of unneutralized de facto probability-raising relative to a model. I will state the definitions and
 321 then show how they work with reference to the three examples that were introduced in Section 3. The
 322 definitions are as follows.^{20,21}

AC(S)

Where $x, x' \in \mathcal{R}(X)$ and $y \in \mathcal{R}(Y)$, $X = x$ rather than $X = x'$ is an actual cause (simpliciter) of $Y = y$ in world θ iff $X = x$ and $Y = y$ are the actual values of X and Y in θ and $X = x$ rather than $X = x'$ is an actual cause of $Y = y$ in θ relative to at least one PCM, $\mathcal{M} = \langle \mathcal{V}, \mathcal{R}, \mathcal{C}, \Omega, \mathcal{F}, do(\cdot) \rangle$ (with $X, Y \in \mathcal{V}$), that is appropriate for evaluating whether $X = x$ rather than $X = x'$ is an actual cause (simpliciter) of $Y = y$ in θ .

AC(M-R)

Where $x, x' \in \mathcal{R}(X)$ and $y \in \mathcal{R}(Y)$, $X = x$ rather than $X = x'$ is an actual cause of $Y = y$ relative to a model $\mathcal{M} = \langle \mathcal{V}, \mathcal{R}, \mathcal{C}, \Omega, \mathcal{F}, do(\cdot) \rangle$ (with $X, Y \in \mathcal{V}$) in world θ iff there is a partition (\mathbf{Z}, \mathbf{W}) of $\mathcal{V} \setminus X, Y$ such that, where $\mathbf{W} = \mathbf{w}^*$ are the actual values the variables in \mathbf{W} take in θ , for all subsets \mathbf{Z}' of \mathbf{Z} (where $\mathbf{Z}' = \mathbf{z}^*$ are the actual values that the variables in \mathbf{Z}' take in θ):

$$P(Y = y | do(X = x \& \mathbf{W} = \mathbf{w}^* \& \mathbf{Z}' = \mathbf{z}^*)) > P(Y = y | do(X = x' \& \mathbf{W} = \mathbf{w}^*)) \quad (\text{IN})$$

323 In **AC(M-R)**, the variables in \mathbf{W} correspond to the ‘background’ that is held fixed in looking for *de facto*
 324 probability-raising of $Y = y$ by $X = x$ (rather than $X = x'$). Against that background, the variables in
 325 \mathbf{Z} are the potential neutralizers of any such de facto probability-raising.

326 In an appropriate causal model we can try each and every partition of the variables into
 327 background and potential neutralizers in looking for unneutralized de facto probability-raising of
 328 $Y = y$ by $X = x$ (rather than $X = x'$). According to **AC(M-R)** the existence of one such partition is
 329 all that is needed for model-relative actual causation, and according to **AC(S)** the existence of actual
 330 causation relative to at least one appropriate model is all that is needed for actual causation *simpliciter*.
 331 What we will see in what follows is that we have the best chance of identifying unneutralized de facto

²⁰ Those familiar with Halpern and Pearl’s ([8], [9]) analyses of deterministic actual causation are invited to see an analogy between their analyses and **AC(M-R)**. **AC(M-R)** was partly inspired by thinking about how a counterpart of Halpern and Pearl’s analysis might be developed that is adequate to the probabilistic case. (In fact, there is a disanalogy to Halpern and Pearl’s definitions, and an analogy to that given by Halpern in his [51] in that the following analysis requires that the variables in \mathbf{W} be held fixed at their actual values – a requirement that will be discussed further in Subsection 7.2 and Subsection 7.3 below. Still, the following analysis, unlike that given in Halpern’s [51] incorporates a condition that is analogous to Halpern and Pearl’s AC2(b). This is indispensable in the probabilistic case because it allows us to deal with fizzling.) I think that the following definitions are adequate to cover deterministic actual causation as the special case where all probabilities are 1 or 0. This is why my definitions take the definiendum to be ‘actual cause’ rather than ‘probabilistic actual cause’.

²¹ Note that relativity to a world θ is invoked in three ways in the definition **AC(S)** of actual cause (simpliciter). First, directly, because **AC(S)** requires that $X = x$ and $Y = y$ to be the values X and Y take in θ if they are to be actual cause and effect in θ . Second, indirectly, because **AC(S)** invokes the notion of model-relative actual causation defined by **AC(M-R)**, and **AC(M-R)** takes model-relative actual causation to itself be a world-relative matter. That’s because **AC(M-R)** invokes the *actual values* that the variables in \mathbf{Z} and \mathbf{W} take in θ . Third, again indirectly, because **AC(S)** invokes the notion of an *appropriate* PCM and the latter is a world-relative notion because whether a model satisfies (Veridicality) (and perhaps (Serious Possibilities)) is world-relative.

332 probability-raising relative to a model where we allocate to \mathbf{Z} all the variables that lie on one or more
 333 paths from X to Y in the graph associated with that model and where we allocate to \mathbf{W} all the variables
 334 that lie off those paths.

335 Briefly,²² the reason for this is that a directed path from X to Y can be thought of as representing
 336 an actual or potential causal process connecting the two variables. We therefore won't find de facto
 337 probability-raising if we hold fixed intermediate variables on all paths between X and Y , since this
 338 will serve to 'screen off' the values of Y from those of X . On the other hand, when we find de facto
 339 probability-raising along paths from X to Y by holding off-path variables fixed, this is prima facie
 340 evidence that the paths represents active causal processes from X to Y . However, these processes
 341 might be fizzled, in which case actual values of variables on those paths will serve as neutralizers.

342 Still, these definitions can best be understood by seeing how they work. Their workings can be
 343 illustrated with respect to the three examples introduced in Section 3.

344 6.1. Fizzling

345 **AC(M-R)** counts $M = 1$ as *not* being an actual cause of $E = 1$ relative to $\mathcal{M}_{\mathbf{Fiz}}$ (and the world described
 346 in **Fizzling**). To see this, consider the partition of $\mathcal{V}_{\mathbf{Fiz}} \setminus M, E$ in which $\mathbf{W} = \emptyset$ and $\mathbf{Z} = \{T\}$. Relative to
 347 this model and this partition, **(IN)** is not satisfied for the subset $\mathbf{Z}' = \{T\}$. That's because Equality (3)
 348 holds.

349 Since there's only one variable in $\mathcal{V}_{\mathbf{Fiz}} \setminus M, E$ – namely, T – there's only one other partition of the
 350 variables in $\mathcal{V}_{\mathbf{Fiz}} \setminus M, E$ to consider when looking for unneutralized de facto probability-raising of $E = 1$
 351 by $M = 1$ relative to $\mathcal{M}_{\mathbf{Fiz}}$: namely that in which T is assigned to \mathbf{W} rather than \mathbf{Z} . But unneutralized
 352 de facto probability-raising isn't revealed by this assignment either. That's because the value of T
 353 'screens off' M from E , so when the value of T is held fixed as part of the assignment $\mathbf{W} = \mathbf{w}^*$, varying
 354 the value of M doesn't make a difference to the probability of $E = 1$, and so **(IN)** doesn't hold for the
 355 null subset of \mathbf{Z} .

356 Given that **(IN)** isn't satisfied for every subset of \mathbf{Z} relative to any partition of the variables in
 357 $\mathcal{V}_{\mathbf{Fiz}} \setminus M, E$, **AC(M-R)** doesn't count $M = 1$ as an actual cause of $E = 1$ relative to $\mathcal{M}_{\mathbf{Fiz}}$. The question
 358 is whether **AC(M-R)** counts $M = 1$ as an actual cause of $E = 1$ relative to *any* appropriate model (as is
 359 required for **AC(S)** to count $M = 1$ as an actual cause of $E = 1$ *simpliciter*). In showing that it doesn't, it
 360 will be helpful to note that a model $\mathcal{M}_{\mathbf{Fiz}}^{T_{fine}}$ that differs from $\mathcal{M}_{\mathbf{Fiz}}$ only by replacing T with a variable
 361 T_{fine} that represents the possible Geiger counter readings as finely as possible (i.e. T_{fine} has a value
 362 corresponding to each possible precise reading of the Geiger counter) is also not one relative to which
 363 **AC(M-R)** counts $M = 1$ as an actual cause of $E = 1$. That's because, just as the actual value of T serves
 364 to screen off M from E if held fixed as one of the background variables \mathbf{W} and neutralizes the (de facto)
 365 probability-raising of $E = 1$ by $M = 1$ if included in \mathbf{Z} , so too does the actual value – $T_{fine} = t_{fine}^*$ – of
 366 T_{fine} (which of course represents a reading of the Geiger counter that lies below the threshold reading).

367 Next, note that $\mathcal{M}_{\mathbf{Fiz}}$ clearly satisfies (Partition) and (Independence). By stipulation, it satisfies
 368 (Veridicality) relative to the world described in **Fizzling**. Although (Naturalness) and (Serious
 369 Possibilities) are somewhat vague requirements, it seems clear that $\mathcal{M}_{\mathbf{Fiz}}$ isn't a borderline case, but
 370 rather clearly satisfies them (certainly it doesn't represent the sort of possibilities or unnatural states of
 371 affairs that these requirements are designed to deal with in the deterministic actual causation/SEM
 372 literature – cf. 49). $\mathcal{M}_{\mathbf{Fiz}}^{T_{fine}}$ also satisfies each of these conditions. Since $\mathcal{M}_{\mathbf{Fiz}}$ and $\mathcal{M}_{\mathbf{Fiz}}^{T_{fine}}$ satisfy these
 373 requirements, no model relative to which **AC(M-R)** is satisfied, but that has a variable set that is a
 374 strict subset of $\mathcal{V}_{\mathbf{Fiz}}$ or $\mathcal{M}_{\mathbf{Fiz}}^{T_{fine}}$ will count as 'appropriate', because it will not satisfy (Stability).

375 But, among models whose variable sets are not strict subsets of $\mathcal{V}_{\mathbf{Fiz}}$ or $\mathcal{M}_{\mathbf{Fiz}}^{T_{fine}}$, is there any
 376 appropriate one relative to which model **AC(M-R)** is satisfied? That is, is there any appropriate

²² More detail on this can be found in (10, 44, and 9, Appendix A.1).

377 model and partition (\mathbf{W} , \mathbf{Z}) of that model's variable set (excluding M and E) relative to which (**IN**) is
 378 satisfied for every subset of \mathbf{Z} ? The answer is 'no'. To see this suppose that a model satisfying (Serious
 379 Possibilities), (Partition), (Independence), (Naturalness), (Veridicality) (hereafter abbreviated 'SPINV')
 380 includes T (or T_{fine}) in its variable set. Then, since T (T_{fine}) 'screens off' M from E , T (T_{fine}) will have
 381 to be included as an element of \mathbf{Z} rather than \mathbf{W} in any partition of the model's variable set if that
 382 partition is to reveal de facto probability-raising of $E = 1$ by $M = 1$. Now consider the subset $\mathbf{Z}' = T$
 383 ($\mathbf{Z}' = T_{fine}$) of \mathbf{Z} . Because $M = 1$ is only relevant to $E = 1$ because it is relevant to the Geiger counter
 384 reading exceeding the threshold, the probability of $E = 1$ when $M = 1$ and T (T_{fine}) takes its actual
 385 value $T = 0$ ($T_{fine} = t_{fine}^*$) is no higher than the probability of $E = 1$ when simply $M = 0$, no matter
 386 what other variables we might care to include in the model and hold fixed as part of \mathbf{W} .

387 So **AC(M-R)** doesn't count $M = 1$ as an actual cause of $E = 1$ relative to any model with T (or
 388 T_{fine}) in its variable set. This means that any otherwise appropriate model (i.e. any model satisfying
 389 SPINV) $\mathcal{M}'_{\text{Fiz}}$ relative to which $M = 1$ is an actual cause of $E = 1$ can be expanded to a model $\mathcal{M}'_{\text{Fiz}}{}^{+T}$
 390 (or $\mathcal{M}'_{\text{Fiz}}{}^{+T_{fine}}$) relative to which $M = 1$ isn't an actual cause of $E = 1$ simply by the addition of T (T_{fine}).
 391 Provided that $\mathcal{M}'_{\text{Fiz}}{}^{+T}$ ($\mathcal{M}'_{\text{Fiz}}{}^{+T_{fine}}$) satisfies SPINV, $\mathcal{M}'_{\text{Fiz}}$ violates (Stability) and is inappropriate. So
 392 **AC(S)** will correctly *not* count $M = 1$ as an actual cause *simpliciter* of $E = 1$.

393 Since the values of T (T_{fine}) form a partition and represent natural states of affairs, (Partition)
 394 and (Naturalness) will be satisfied by $\mathcal{M}'_{\text{Fiz}}{}^{+T}$ (or $\mathcal{M}'_{\text{Fiz}}{}^{+T_{fine}}$) if they were satisfied by $\mathcal{M}'_{\text{Fiz}}$. Moreover,
 395 it doesn't seem that a variable representing possible readings of the Geiger counter in **Fizzling** can
 396 represent the sort of non-serious possibilities that (Serious Possibilities) is intended to rule out by
 397 those who adopt it.²³ So it doesn't seem that $\mathcal{M}'_{\text{Fiz}}{}^{+T}$ (or $\mathcal{M}'_{\text{Fiz}}{}^{+T_{fine}}$) could represent any non-serious
 398 possibilities if $\mathcal{M}'_{\text{Fiz}}$ doesn't.

399 When it comes to (Veridicality), it should be noted that there are multiple ways of expanding
 400 a model $\mathcal{M}'_{\text{Fiz}}$ via the addition of T (T_{fine}), each associated with a different $do(\cdot)$ function implying
 401 different facts about how the probability distribution over T (T_{fine}) depends upon other variables in
 402 the model, and vice versa. In looking for an apt expanded model, we just select the one with the $do(\cdot)$
 403 function that implies the truth (relative to the world we are modelling) about how the objective chance
 404 distribution over T (T_{fine}) depends upon other variable in the model, and vice versa.

405 (Independence) is a little trickier. Might not $\mathcal{M}'_{\text{Fiz}}$ include a variable whose values are logically
 406 or metaphysically related to those of T and T_{fine} ? There two interesting possibilities.²⁴ One of these
 407 is that $\mathcal{M}'_{\text{Fiz}}$ includes a variable T' that's intermediate in grain between T and T_{fine} .²⁵ But then $\mathcal{M}'_{\text{Fiz}}$
 408 itself isn't a model relative to which there's unneutralized de facto probability-raising of $E = 1$ by
 409 $M = 1$. That's because the actual value of T' (representing a state of affairs that is identical to, or a
 410 realizer of, that represented by $T = 0$) screens off M from E and so can't be held fixed as part of \mathbf{W} in

²³ True, if T_{fine} represents the full range of possible readings of the Geiger counter, there are some possible readings that will have extremely low probability given that I place my U-232 near to the Geiger counter. Still, whenever (Serious Possibilities) has been invoked in the literature it has been to rule out models containing variables corresponding to certain factors that are both non-salient in some causal story and metaphysically distinct from those that are rendered salient (e.g. McCartney getting in the way of the JFK-bound bullets); it is never to rule out models containing variables that represent salient factors in a fine grained way. Nor do I think there's any need to rule such models out. (Indeed, it would strike me as very troubling – especially in light of the discussion of Subsection 7.1 below – if an account of actual causation depended for its success on not representing factors acknowledged to be relevant in too detailed a way.) So I will interpret (Serious Possibilities) as not ruling them out.

²⁴ The third, non-interesting possibility is one where $\mathcal{M}'_{\text{Fiz}}$ includes a variable or variables representing gerrymandered states of affairs that are logically/metaphysically related to those represented by T and T_{fine} – e.g. T_{gerry} , which takes value $T_{gerry} = 1$ if the Geiger counter threshold is reached or Trump is US president, and $T_{gerry} = 0$ otherwise. Such a model would straightforwardly violate (Naturalness) and so even if $M = 1$ counted as an actual cause of $E = 1$ relative to it, it could not be inferred that $M = 1$ is an actual cause of $E = 1$ *simpliciter*.

²⁵ Since T is a binary variable, and since T_{fine} represents the Geiger counter reading in the finest possible way, $\mathcal{M}'_{\text{Fiz}}$ couldn't contain a coarse-graining of T or a fine-graining of T_{fine} .

411 the partition of the variable set of $\mathcal{M}'_{\text{Fiz}}$ if de facto probability-raising is to be revealed. Moreover (if
 412 included in \mathbf{Z}) the actual value of T' neutralizes any de facto probability-raising of $E = 1$ by $M = 1$.

413 A second possibility is that $\mathcal{M}'_{\text{Fiz}}$ contains a variable T_{cross} , the values of which are not all realizers
 414 of the values of T , but where there is some 'cross-cutting' of them. For instance, it might be that T_{cross} is
 415 a ternary variable, with one value representing an interval of Geiger counter readings from 0 to some
 416 value n well below the threshold, a second value representing an interval of readings from some value
 417 m well above the threshold and upward, and a third value representing the interval of readings (n, m) .
 418 If the actual reading of the Geiger counter lay in (n, m) then the actual value of T_{cross} wouldn't serve
 419 as a neutralizer for any de facto probability-raising of $E = 1$ by $M = 1$ revealed in $\mathcal{M}'_{\text{Fiz}}$ (as it would,
 420 for instance, be relative to the partition $\mathbf{W} = \emptyset, \mathbf{Z} = \{T_{\text{cross}}\}$ of $\mathcal{V}'_{\text{Fiz}} \setminus M, E$ if $\mathcal{V}'_{\text{Fiz}} = \{M, T_{\text{cross}}, E\}$), and
 421 we couldn't simply add T or T_{fine} to the model to show that the model violates (Stability), since the
 422 result would not be a model that satisfied (Independence). However, in such a case, the model *would*
 423 violate (Stability) because, since it represents the Geiger counter reading as finely as possible, T_{fine}
 424 is a fine-graining of T_{cross} and replacing T_{cross} with T_{fine} would (for reasons explained above) yield a
 425 model in which there's no unneutralized de facto probability-raising of $E = 1$ by $M = 1$.

426 So any model that satisfies SPINV relative to which $M = 1$ counts as an actual cause of $E = 1$
 427 violates (Stability) so that **(AC(S))** yields the correct result that $M = 1$ is not an actual cause of $E = 1$
 428 *simpliciter*.

429 6.2. Probabilistic Preemption

430 6.2.1. $M = 1$ is an actual cause (simpliciter) of $E = 1$ in Probabilistic Preemption

431 **AC(M-R)** counts $M = 1$ as an actual cause of $E = 1$ relative to $\mathcal{M}_{\text{ProbPre}}$ (and the world described in
 432 **Probabilistic Preemption**). To see this, consider the partition of $\mathcal{V}_{\text{ProbPre}} \setminus M, E$ such that $\mathbf{W} = \{D, Y\}$
 433 and $\mathbf{Z} = \{T\}$. **AC(M-R)** is satisfied because **(IN)** holds for both subsets of \mathbf{Z} (\emptyset and $\{T\}$), as shown by
 434 inequalities 9 and 10:

$$P(E = 1 | do(M = 1 \& D = 1 \& Y = 0)) > P(E = 1 | do(M = 0 \& D = 1 \& Y = 0)) \quad (9)$$

$$P(E = 1 | do(M = 1 \& T = 1 \& D = 1 \& Y = 0)) > P(E = 1 | do(M = 0 \& D = 1 \& Y = 0)) \quad (10)$$

435 Inequality 9 indicates that my action raises the probability of the explosion *holding fixed* that (you make
 436 your decision but) don't place your Th-228 near to the Geiger counter. The existence of this *de facto*
 437 probability-raising reflects the fact that there's a path – $\langle M, T, E \rangle$ – along which $M = 1$ promotes $E = 1$
 438 ($M = 1$ raises the probability of $E = 1$ when we hold fixed the values of all variables off that path).

439 Inequality 10 indicates that, again holding fixed $D = 1$ and $Y = 0$, the probability of $E = 1$ is
 440 higher if I place my U-232 near the Geiger *and the threshold reading is reached* (as is actually the case in
 441 **Probabilistic Preemption**) than if I'd not placed my U-232 near to the Geiger counter. This reflects the
 442 fact that, not only is there a potential process via which $M = 1$ threatens to bring about $E = 1$, but an
 443 important part of that process (namely: the Geiger counter threshold being reached) occurs.

444 Since **AC(M-R)** implies that $M = 1$ is an actual cause of $E = 1$ relative to $\mathcal{M}_{\text{ProbPre}}$, **AC(S)** yields
 445 the (correct) result that $M = 1$ is an actual cause (simpliciter) of $E = 1$ provided that $\mathcal{M}_{\text{ProbPre}}$ is
 446 appropriate. $\mathcal{M}_{\text{ProbPre}}$ is appropriate. Clearly it satisfies (Partition) and (Independence). It satisfies
 447 (Naturalness) because all of the states that its variables represent are reasonably natural. It was
 448 stipulated that the $do(\cdot)$ function associated with $\mathcal{M}_{\text{ProbPre}}$ is such that (Veridicality) is satisfied
 449 relative to the world described in **Probabilistic Preemption**. Moreover, $\mathcal{M}_{\text{ProbPre}}$ doesn't represent
 450 the sort of 'non-serious' possibility that (Serious Possibilities) is introduced to rule out (cf. 10; 12, pp.
 451 86-91).

452 Finally, (Stability) is satisfied because the causal process from my action to the explosion is
 453 complete. Holding fixed $D = 1$ and $Y = 0$, the probability of the explosion if $M = 1$ and parts of this
 454 process occur is higher than the probability of the explosion if simply $M = 0$. Any variable (whose
 455 values represent reasonably natural states, form a partition, and are logically and metaphysically
 456 independent from the variables in $\mathcal{V}_{\text{ProbPre}}$) that might be added to $\mathcal{V}_{\text{ProbPre}}$ either represents part of
 457 this process or it doesn't. If it does, its actual value represents *the occurrence* of part of the process
 458 (since in **Probabilistic Preemption** this process is complete). So, if it is added to $\mathcal{V}_{\text{ProbPre}}$, including it
 459 in \mathbf{Z} will not prevent (IN) from holding for all subsets \mathbf{Z}' of \mathbf{Z} . If it doesn't, then adding it to $\mathcal{V}_{\text{ProbPre}}$,
 460 including it in \mathbf{W} , and holding it fixed at its actual value as part of the assignment $\mathbf{W} = \mathbf{w}^*$ will not
 461 make a difference to the fact that (IN) holds for all subsets \mathbf{Z}' of \mathbf{Z} , since holding fixed $Y = 0$ as part
 462 of $\mathbf{W} = \mathbf{w}'$ is already sufficient to ensure this. Either way, there's a partition of the resulting model's
 463 variable set relative to which a relation of unneutralized de facto probability-raising of $E = 1$ by $M = 1$
 464 is revealed. **AC(M-R)** requires the existence of only one such partition for $M = 1$ to count as an actual
 465 cause of $E = 1$ relative to this richer model. So any such richer model is one relative to which $M = 1$
 466 is an actual cause of $E = 1$, meaning that (Stability) is satisfied by $\mathcal{M}_{\text{ProbPre}}$, and **AC(S)** therefore
 467 correctly counts $M = 1$ as an actual cause of $E = 1$ *simpliciter*.

468 Note that **Probabilistic Preemption** is an *early* preemption case. It could be changed to a case of
 469 *late* preemption by supposing that you decide, not to place your Th-228 near to the Geiger counter iff I
 470 don't place my U-232 near to the Geiger counter, but rather that you will place your Th-228 near to
 471 the Geiger counter iff *the bomb doesn't explode*. Still, in the scenario where I place my U-232 near to the
 472 Geiger counter, the threshold is reached and the bomb explodes (and you don't place your Th-228 near
 473 to the Geiger counter), my action is an actual cause of the explosion.

474 We can model this case using the variable set $\mathcal{V}_{\text{LatePre}} = \{M, Y, D', T, E\}$, with M, Y, T , and E
 475 given the same interpretations as in $\mathcal{M}_{\text{ProbPre}}$, but with D' given a slightly different interpretation
 476 than that given to the variable D in $\mathcal{M}_{\text{ProbPre}}$: specifically D' takes value $D' = 1$ if you decide that you
 477 will place your Th-228 near to the Geiger counter iff *the bomb doesn't explode*; and value $D' = 0$ if you
 478 don't make that decision. Combined with the veridical $do(\cdot)$ function for this variable set and this
 479 scenario, we arrive at a model $\mathcal{M}_{\text{LatePre}}$. But it is easy to verify that the above reasoning that shows that
 480 **AC(M-R)** counts $M = 1$ as an actual cause of $E = 1$ relative to $\mathcal{M}_{\text{ProbPre}}$ isn't sensitive to the difference
 481 between $\mathcal{M}_{\text{ProbPre}}$ and $\mathcal{M}_{\text{LatePre}}$. And the reasoning that shows that $\mathcal{M}_{\text{ProbPre}}$ is an appropriate model
 482 can be carried across to $\mathcal{M}_{\text{LatePre}}$ just by making the relevant substitutions. Consequently **AC(S)**
 483 correctly counts $M = 1$ as an actual cause of $E = 1$ in this late preemption scenario. In Subsection 6.2.3
 484 below, we'll see that it also correctly discounts $D' = 1$ as an actual cause of $E = 1$ in this scenario.

485 6.2.2. $M = 1$ isn't an actual cause of $E = 1$ in *Fizzled Preemption*

486 It was observed above that $\mathcal{M}_{\text{ProbPre}}$ also serves as a model for **Fizzled Preemption**. However, in this
 487 case we find that the de facto probability-raising of $E = 1$ by $M = 1$ that is revealed by the partition
 488 of $\mathcal{V}_{\text{ProbPre}} \setminus M, E$ such that $\mathbf{W} = \{D, Y\}$ and $\mathbf{Z} = \{T\}$ (and indicated by Inequality 9) is neutralized
 489 because the actual value of T is in this case $T = 0$ and Inequality 11 holds:

$$P(E = 1 | do(M = 1 \& T = 0 \& D = 1 \& Y = 0)) \leq P(E = 1 | do(M = 0 \& D = 1 \& Y = 0)) \quad (11)$$

490 Is there an alternative way of partitioning $\mathcal{V}_{\text{ProbPre}} \setminus M, E$ so as to reveal contingent
 491 probability-raising that isn't neutralized in **Fizzled Preemption**? (There need only be *one* such partition
 492 for **AC(M-R)** to be satisfied.) There isn't. Suppose that we assign T to \mathbf{W} instead of \mathbf{Z} . This won't help,
 493 since the value of T 'screens off' M from E so (IN) would then not hold for the null subset of \mathbf{Z} . On the
 494 other hand, suppose that we leave T in \mathbf{Z} and reassign D to \mathbf{Z} (we have to leave Y in \mathbf{W} in order to
 495 reveal de facto probability-raising of $E = 1$ by $M = 1$). In that case, since $M = 1$ only de facto raises

496 the probability of $E = 1$ because of its relevance to T , the fact that $T = 0$ will continue to neutralize
 497 this de facto probability-raising so that (IN) won't hold for the subset $Z' = \{T\}$ of Z .

498 So for **Fizzled Preemption**, there's no partition of $\mathcal{V}_{\text{ProbPre}} \setminus M, E$ such that (IN) is satisfied for
 499 all subsets of Z when we consider $M = 1$ as a putative cause of $E = 1$. **AC(M-R)** therefore doesn't
 500 count $M = 1$ as an actual cause of $E = 1$ relative to $\mathcal{M}_{\text{ProbPre}}$ and the world described by **Fizzled**
 501 **Preemption**.

502 But for **AC(S)** to count $M = 1$ as an actual cause of $E = 1$ *simpliciter*, there need only be one
 503 appropriate model relative to which **AC(M-R)** counts $M = 1$ as an actual cause of $E = 1$. Is there such
 504 a model? There isn't. Suppose a candidate such model includes T . Because M is only relevant to E
 505 because of its relevance to T , the value of T 'screens off' the value of M from that of E . This means that,
 506 if T is included in \mathbf{W} in the partition (\mathbf{W}, \mathbf{Z}) of that model's variable set and held fixed at the value that
 507 it actually takes in **Fizzled Preemption** – namely, $T = 0$ – as part of the assignment $\mathbf{W} = \mathbf{w}^*$, then (IN)
 508 won't be satisfied for the empty subset of Z . Alternatively, if T is included in Z then, no matter what
 509 other variables are included in the model and assigned to \mathbf{W} , (IN) won't be satisfied for the subset $\{T\}$
 510 of Z . This is because $M = 1$ only threatens to bring about $E = 1$ because it threatens to bring about
 511 $T = 1$, so no matter what we hold fixed by inclusion on both sides of (IN), the probability of $E = 1$ is
 512 no higher if $M = 1$ and $T = 0$ than if simply $M = 0$.

513 So **AC(M-R)** doesn't count $M = 1$ as an actual cause of $E = 1$ relative to any appropriate model
 514 with T in its variable set. Note that the same reasoning, *mutatis mutandis*, shows that, equally, **AC(M-R)**
 515 doesn't count $M = 1$ as an actual cause of $E = 1$ relative to any appropriate model with T_{fine} in its
 516 variable set. This means that any otherwise appropriate model relative to which $M = 1$ is an actual
 517 cause of $E = 1$ can be expanded to a model in which $M = 1$ isn't an actual cause of $E = 1$ simply
 518 by the addition of T (T_{fine}). Provided that the expanded model is appropriate, the original model
 519 violates (Stability) and so is inappropriate. So **AC(S)** will correctly not count $M = 1$ as an actual cause
 520 *simpliciter* of $E = 1$ relative to the world described by **Fizzled Preemption**.

521 Since the values of T (T_{fine}) form a partition and represent natural states of affairs, (Partition)
 522 and (Naturalness) will be satisfied by the expanded model if they were satisfied by the original model.
 523 Moreover, it doesn't seem that a variable representing possible readings of the Geiger counter can
 524 represent the sort of non-serious possibilities that (Serious Possibilities) is intended to rule out by those
 525 who adopt it. With regard to (Veridicality), it should be noted that there are multiple ways of expanding
 526 the original model via the addition of T (T_{fine}), each associated with a different *do*(\cdot) function that
 527 entails different facts about how interventions on T (T_{fine}) affect the probability distribution over the
 528 remaining variables in the model, and vice versa. In looking for an apt expanded model, we just select
 529 the one with the *do*(\cdot) function that returns the true objective chances in the world described by **Fizzled**
 530 **Preemption**. Where this is so, (Veridicality) will be satisfied but also the actual value of T (T_{fine}) will
 531 screen off M from E – if T (T_{fine}) is included in \mathbf{W} – or neutralize any de facto probability-raising of
 532 $E = 1$ by $M = 1$ – if T (T_{fine}) is included in Z .

533 With regard to (Independence), suppose the original model includes a variable T' that's
 534 intermediate in grain between T and T_{fine} . Then the original model itself isn't one relative to which
 535 there's unneutralized de facto probability-raising of $E = 1$ by $M = 1$. That's because the actual value of
 536 T' screens off M from E and so can't be held fixed as part of \mathbf{W} in the partition of the original model's
 537 variable set in looking for de facto probability-raising. Moreover (if included in Z) the actual value of
 538 T' neutralizes any de facto probability-raising of $E = 1$ by $M = 1$.

539 A second possibility is that the original model contains a variable T_{cross} the values of which are
 540 not all realizers of the values of T but where there is some 'cross-cutting' of them (of the sort described
 541 in Subsection 6.1 above). In such a case, we couldn't simply add T or T_{fine} to the model to show that
 542 the model violates (Stability) since the result would be a model that doesn't satisfy (Independence).
 543 But, in such a case, the model would nevertheless violate (Stability) because, since it represents the
 544 Geiger counter reading as finely as possible, T_{fine} is a fine-graining of T_{cross} and replacing T_{cross} with

545 T_{fine} would yield a model in which there's no unneutralized de facto probability-raising of $E = 1$ by
 546 $M = 1$.

547 So any model that satisfies SPINV relative to which $M = 1$ counts as an actual cause of $E = 1$
 548 violates (Stability) for the world described by **Fizzled Preemption**, so that **AC(S)** yields the correct
 549 result that $M = 1$ is not an actual cause of $E = 1$ *simpliciter*.

550 6.2.3. $D = 1$ isn't an actual cause of $E = 1$ in **Probabilistic Preemption** or **Fizzled Preemption**

551 It is also worth observing that **AC(S)** gives the verdict that $D = 1$ is *not* an actual cause of $E = 1$
 552 relative to either the world described by **Probabilistic Preemption** or the world described by **Fizzled**
 553 **Preemption**. The same considerations show that this is true for both worlds, since the actual value
 554 of T – which is the key difference between these worlds – doesn't play any part in the reasoning that
 555 shows this to be so. This reasoning is as follows.

556 For **AC(S)** to count $D = 1$ as an actual cause of $E = 1$ *simpliciter* there must be an appropriate
 557 model relative to which **AC(M-R)** counts $D = 1$ as an actual cause of $E = 1$. But there isn't such a
 558 model. To see this, first suppose a candidate such model includes Y in its variable set. Because D is
 559 only relevant to E because of its relevance to Y , the value of Y 'screens off' the value of D from that of E .
 560 This means that, if Y is included in \mathbf{W} in the partition (\mathbf{W}, \mathbf{Z}) of the model's variable set and held fixed
 561 at its actual value ($Y = 0$) as part of the assignment $\mathbf{W} = \mathbf{w}^*$, then **(IN)** won't be satisfied for the empty
 562 subset of \mathbf{Z} . Alternatively, if Y is included in \mathbf{Z} then, no matter what other variables are included in the
 563 model and assigned to \mathbf{W} , **(IN)** won't be satisfied for the subset $\{Y\}$ of \mathbf{Z} . Specifically, because $D = 1$
 564 only threatens to bring about $E = 1$ because it threatens to bring about $Y = 1$, no matter what we hold
 565 fixed by inclusion on both sides of **(IN)** (provided it's not some gerrymandered state of affairs that's
 566 metaphysically related to D and/or E – such as *your-not-making-the-decision-or-the-bomb's-exploding* – in
 567 which case the model would violate (Naturalness) and (Independence)), the probability of $E = 1$ is no
 568 higher if $D = 1$ and $Y = 0$ than if simply $D = 0$.

569 So **AC(M-R)** doesn't count $D = 1$ as an actual cause of $E = 1$ relative to any appropriate model
 570 with Y in its variable set. Note that the same reasoning, *mutatis mutandis*, shows that equally **AC(M-R)**
 571 doesn't count $M = 1$ as an actual cause of $E = 1$ relative to any appropriate model with Y_{fine} in its
 572 variable set, where Y_{fine} includes values representing precisely how far you place your Th-228 from
 573 the Geiger (perhaps up to some threshold $\gg 5cm$, with a value reserved to represent your not placing
 574 your Th-228 within that threshold distance at all). This means that any otherwise appropriate model
 575 relative to which $D = 1$ is an actual cause of $E = 1$ can be expanded to a model in which $D = 1$ isn't
 576 an actual cause of $E = 1$ simply by the addition of Y (or Y_{fine}). Provided that the expanded model is
 577 appropriate, the original model violates (Stability) and is inappropriate so **AC(S)** will correctly not
 578 count $D = 1$ as an actual cause *simpliciter* of $E = 1$.

579 Since the values of Y (Y_{fine}) form a partition and represent reasonably natural states of affairs,
 580 (Partition) and (Naturalness) will be satisfied by the expanded model if they were satisfied by the
 581 original model. Neither Y nor Y_{fine} appears to introduce the sort of possibility that (Serious Possibilities)
 582 was introduced to rule out by those who endorse it. So it doesn't seem that the expanded model could
 583 violate (Serious Possibilities) if the original model doesn't. With regard to (Veridicality), it should
 584 be noted that there are multiple ways of expanding the original model via the addition of Y (Y_{fine}),
 585 each associated with a different $do(\cdot)$ function that entails different facts about how interventions on Y
 586 (Y_{fine}) affect the probability distribution over the remaining variables in the model, and vice versa. In
 587 looking for an apt expanded model, we just select the one with the $do(\cdot)$ function that returns the true
 588 objective chances in the worlds described by **Probabilistic Preemption** and **Fizzled Preemption** (the
 589 chances were identical in each of these stories, so the true $do(\cdot)$ function is the same for both worlds).
 590 Relative to such a $do(\cdot)$ function, Y (Y_{fine}) screens off D from E and its actual value neutralizes any de
 591 facto probability-raising of $E = 1$ by $D = 1$ that might exist in such a model.

592 (Independence) is a little trickier. Might not the original model include a variable whose
 593 values are logically or metaphysically related to those of Y and Y_{fine} ? If that variable represents

594 reasonably natural states (so that the original model satisfies (Naturalness)), then it seems that
 595 this variable must simply pertain to what you do (it won't have values that represent, say,
 596 *your-placing-your-Th-228-near-to-the-Geiger-counter-or-the-bomb's-exploding*). It might represent what you
 597 do in a more fine-grained way: e.g. it might be the variable Y' , which takes value $Y' = 0$ if you don't
 598 place your Th-228 near to the Geiger counter, $Y' = 1$ if you place it 2.5-5cm from the Geiger counter,
 599 and $Y' = 2$ if you place it 0-2.5cm from the Geiger counter. But then it will also be such that its actual
 600 value – in this case, $Y' = 0$ – screens off D from E (so that de facto probability-raising of $E = 1$ by
 601 $D = 1$ isn't revealed if it is included in \mathbf{W} in the partition of that model's variable set) and fizzles the
 602 process via which your decision threatens to bring about the explosion (so that if it is included in \mathbf{Z}
 603 in the partition of that model's variable set, it serves to neutralize any de facto probability-raising of
 604 $E = 1$ by $D = 1$ that might be revealed via that partition). Either way, this means that **AC(M-R)** isn't
 605 satisfied in the original model.

606 Or it might be that the model contains a variable that has values that represent states that cross-cut
 607 those represented by Y : e.g. it might be a variable Y_{cross} , which takes value $Y_{cross} = 0$ if you don't place
 608 your Th-228 within 7.5 cms of the Geiger counter, $Y_{cross} = 1$ if you place it 2.5-7.5cm from the Geiger
 609 counter, and $Y_{cross} = 2$ if you place it 0-2.5cm from the Geiger counter. In that case, its actual value
 610 might not act as a neutralizer for $D = 1$ and $E = 1$ (specifically it won't if its actual value is $Y_{cross} = 1$).

611 In such a case, we couldn't simply add Y or Y_{fine} to the model to show that it violates (Stability)
 612 since the result would be a model that doesn't satisfy (Independence). But, in such a case, the model
 613 would still in fact violate (Stability) because Y_{fine} is a fine-graining of Y_{cross} and replacing Y_{cross} with
 614 Y_{fine} would, for reasons described above, yield a model in which there's no unneutralized de facto
 615 dependence.

616 So any model that satisfies SPINV relative to which $D = 1$ counts as an actual cause of $E = 1$
 617 violates (Stability) for the world described by **Fizzled Preemption**, so that **AC(S)** yields the correct
 618 result that $D = 1$ isn't an actual cause of $E = 1$ *simpliciter*.

619 Now recall our late preemption case, in which you decide that you'll place your Th-228 near to
 620 the Geiger counter iff *the bomb doesn't explode* (rather than iff I don't place my U-232 near to the Geiger
 621 counter), but in which I place my U-232 near to the Geiger counter, the threshold is reached and the
 622 bomb explodes (and you don't place your Th-228 near to the Geiger counter). It was noted that we can
 623 model this case using the variable set $\mathcal{V}_{LatePre} = \{M, Y, D', T, E\}$, with D' being a variable that takes
 624 value $D' = 1$ if you decide that you'll place your Th-228 near to the Geiger counter iff *the bomb doesn't*
 625 *explode*; and value $D' = 0$ otherwise. $\mathcal{M}_{LatePre}$ is a model arrived at by combining this variable set
 626 with the veridical *do*(\cdot) function for this scenario.

627 Now note that the above reasoning that shows that **AC(M-R)** doesn't count $D = 1$ as an actual
 628 cause of $E = 1$ relative to $\mathcal{M}_{ProbPre}$ isn't sensitive to the difference between $\mathcal{M}_{ProbPre}$ and $\mathcal{M}_{LatePre}$,
 629 nor is the reasoning that shows that any model satisfying SPINV that does count $D = 1$ as an actual
 630 cause of $E = 1$ violates (Stability). Consequently **AC(S)** correctly counts $D' = 1$ as *not being* an actual
 631 cause of $E = 1$ in this late preemption scenario. So **AC(S)** handles this late preemption scenario as well
 632 as the early preemption scenario.

633 7. Further Cases

634 In this section, I will discuss how the present account handles some further cases that have either been
 635 raised as posing problems for existing accounts of probabilistic actual causation or that are analogues
 636 to cases that have been raised as posing problems for accounts of deterministic actual causation, and
 637 so may further test the present account.

638 7.1. Determinable Effects

639 A scenario which poses a prima facie challenge for accounts of probabilistic actual causation is given
 640 by Hitchcock [25, p. 411]:

Determinable Effect

“Barney smokes, and he also spends a lot of time in the sun. These two proclivities are not connected; for example, Barney is not forced to go outside in order to smoke. Barney’s smoking increases the probability that he will get lung cancer. By increasing his probability of getting lung cancer, Barney’s smoking increases the overall probability that he will suffer from some form of cancer, and analogously for his exposure to the sun. In fact, Barney develops skin cancer. A fortiori, Barney develops cancer of some form or other.”

641 Let SM be a binary variable that takes the value $SM = 1$ if Barney smokes and $SM = 0$ if he doesn’t;
 642 let SN be a variable that takes value $SN = 1$ if Barney spends a lot of time in the sun, $SN = 0$ if he
 643 doesn’t;²⁶ and let C be a binary variable that takes value $C = 1$ if Barney develops cancer, and $C = 0$ if
 644 he doesn’t.

645 Now consider a model $\mathcal{M}_{\text{DetEff}}$ with the variable set $\mathcal{V}_{\text{DetEff}} = \{SM, C\}$ and the the veridical
 646 $do(\cdot)$ function for the world described in **Determinable Effect**. Note that $\mathbf{W} = \emptyset, \mathbf{Z} = \emptyset$ is the only
 647 possible partition of $\mathcal{V}_{\text{DetEff}} \setminus SM, C$ and **(IN)** is satisfied for $\mathcal{M}_{\text{DetEff}}$ and this partition in virtue of the
 648 fact that $SM = 1$ straightforwardly raises the probability of $C = 1$. So **AC(M-R)** counts $SM = 1$ as
 649 an actual cause of $C = 1$ relative to $\mathcal{M}_{\text{DetEff}}$. Yet $SM = 1$ is not a genuine actual cause of $C = 1$ in
 650 **Determinable Effect**. That’s because the state represented by $C = 1$ (Barney’s developing cancer) is a
 651 determinable of which the actual determinate (Barney’s developing *skin* cancer) is clearly not an effect
 652 of Barney’s smoking.

653 To see that **AC(S)** gives the correct verdict, consider a variable that’s a fine-graining of C : namely,
 654 C_1 , which represents what type of cancer Barney gets, or whether he doesn’t get cancer at all. For
 655 instance, perhaps $C_1 = 0$ represents his not getting cancer, $C_1 = 1$ represents his developing only
 656 lung cancer, $C_1 = 2$ represents his developing only skin cancer, $C_1 = 3$ represents his developing only
 657 bowel cancer, ... $C_1 = i$ represents his developing only lung and bowel cancer, and so on. $SM = 1$
 658 doesn’t straightforwardly raise the probability of C_1 ’s taking its actual value, $C_1 = 2$. Consequently,
 659 $\mathcal{M}_{\text{DetEff}}$ violates (Stability). Nor is there any reasonably natural state of affairs we could hold fixed
 660 to reveal de facto probability-raising of $C_1 = 2$ by $SM = 1$. This means that any appropriate model
 661 containing C_1 isn’t one relative to which there’s de facto probability-raising of $C_1 = 2$ by $SM = 1$, and
 662 so isn’t one relative to which **AC(M-R)** counts $SM = 1$ is an actual cause of the actual value taken
 663 by C_1 . In consequence, any model that contains C rather than C_1 relative to which there is de facto
 664 probability-raising of $C = 1$ by $SM = 1$ violates (Stability). So **AC(S)** correctly doesn’t count $SM = 1$
 665 as an actual cause of $C = 1$.

666 7.2. Overdetermination of Probabilities

667 **AC(M-R)** requires that the variables \mathbf{W} be held fixed at their actual values in seeking de facto
 668 probability-raising and therefore model-relative actual causation. In this respect, it’s more analogous
 669 to the analysis of deterministic actual causation given in [51] than that given in [8] and [9].

670 Is there a case for relaxing this requirement? The principal motive for considering a relaxation
 671 comes from cases where the probability of an effect is *overdetermined*. Cases where an *effect* is
 672 overdetermined – oft discussed in the literature on deterministic causation (the *locus classicus* being [23,
 673 pp. 207-12]) – are the special case in which the probability of the effect is, as it were, overdetermined to
 674 be 1.²⁷ Deterministic preemption cases are a species of overdetermination, but here what I have in

²⁶ We could have let SM be a more *fine grained* variable representing *how much* Barney smokes, and SN be a fine-grained variable representing *how much* time he spends in the sun. This would not substantively affect the analysis, except that we’d need to explicitly state the contrasts in evaluating actual causal claims relative to the example (e.g. ‘Barney’s spending an average of 1000 hours per year in the sun *rather than fewer* was an actual cause of his developing cancer’).

²⁷ Hitchcock [11, p. 512] takes the view that ‘trumping’ cases – as described by Schaffer [52] – are simply overdetermination cases. I agree and I think that attempts to give probabilistic variants of trumping scenarios will simply issue in cases like

675 mind are cases where it would be intuitively wrong to say that some of the overdeterminers are causes
 676 whereas others are not (in preemption cases the preemptor is a cause, while the preempted backup isn't
 677 a cause). This sort of case is often referred to as 'symmetric overdetermination' in the deterministic
 678 causation literature.²⁸

679 The following is a case of overdetermination of probabilities where those probabilities aren't 1s or
 680 0s. I don't claim that the example is physically realistic, but it serves to illustrate a type of probabilistic
 681 causal structure that seems possible in principle.

Overdetermination of Probabilities

Someone (neither you nor I) has connected a Geiger counter to a bomb so that the bomb will explode if the Geiger counter registers above a threshold reading. I place a chunk of U-232 near to the Geiger counter at the same time as you place an identical chunk of U-232 (one comprising exactly the same number of atoms) at an identical distance. The chance of the threshold being reached if either of us alone had placed our U-232 chunks near to the Geiger counter would have been 0.8. Now suppose that, because of their electric charge, alpha particles approaching a location (specifically: the Geiger counter sensor) from two different sources have a propensity to deflect one another from that location. And suppose that the interference between the alpha particles emitted by the two sources is such as to exactly offset the doubled quantity of radioactive material that is present (compared with a scenario in which one of us alone had placed our U-232 near to the Geiger counter), so that the chance of the threshold reading being reached given that we both place our U-232 chunks is identical to the chance of its being reached if either of us had alone placed our U-232 near to the Geiger counter: namely, 0.8. Let us additionally suppose (for simplicity) that each of us was antecedently certain to place our U-232 near to the Geiger counter. Finally, let us suppose that in fact enough non-deflected alpha particles – including some from each source – arrive at the Geiger sensor that the threshold reading is reached and the bomb explodes.

682 It seems definitely wrong to say that, in **Overdetermination of Probabilities**, one of our actions
 683 was an actual cause of the bomb's exploding, while the other's wasn't. However, neither action raises
 684 the probability of the bomb's exploding. Specifically, where E , M , and Y have the usual interpretations,
 685 the following equality holds:²⁹

$$P(E = 1|do(M = 1)) = P(E = 1|do(M = 0)) = P(E = 1|do(Y = 1)) = P(E = 1|do(Y = 0)) = 0.8 \quad (12)$$

686 Note also that, in this case, de facto probability-raising of $E = 1$ by $M = 1$ can't be revealed by
 687 holding fixed Y at its actual value, $Y = 1$. Nor can de facto probability-raising of $E = 1$ by $Y = 1$ be
 688 revealed by holding fixed M at its actual value $M = 1$. Specifically, the following two equalities hold:

$$P(E = 1|do(M = 1 \& Y = 1)) = P(E = 1|do(M = 0 \& Y = 1)) = 0.8 \quad (13)$$

those described in this section, or in cases in which multiple causes raise the probability of their effects (and therefore de facto do so) in a way that isn't neutralized. So I don't think a discussion of these cases would add anything interesting.

²⁸ I prefer to try to avoid this terminology, however, because there are cases of the phenomenon that aren't particularly symmetric. For instance, Assassin B decides she'll shoot at Victim iff Assassin A does so. Assassin A is located much further away from Victim than is Assassin B. Seeing the puff of smoke from A's gun, B shoots at Victim. Because of the shorter distance between them, B's bullet pierces Victim's heart simultaneous with A's bullet. A and B's shots overdetermine Victim's death and it seems wrong to say that one is a cause and the other isn't. But there are clear asymmetries in that B's shot occurs later than, and depends upon, A's shot.

²⁹ Although the example has been constructed so that our actions individually make no difference to the probability (the probability is 'overdetermined'), it could easily be transformed into an example in which each of our acts lowers the probability of the explosion by supposing the interference between the sources is stronger still. Making this alternative assumption makes no difference to the way in which **AC(M-R)** and **AC(S)** diagnose the case.

$$P(E = 1|do(Y = 1 \& M = 1)) = P(E = 1|do(Y = 0 \& M = 1)) = 0.8 \quad (14)$$

689 In general, it seems the only way that we could reveal a latent probability-raising of $E = 1$ by $M = 1$
 690 is by holding fixed Y at its non-actual value $Y = 0$, and likewise the only way that we could reveal
 691 latent probability-raising of $E = 1$ by $Y = 1$ is by holding fixed M at its non-actual value $M = 0$. Thus
 692 (assuming that the probability of the bomb's spontaneously exploding is 0.00001):

$$P(E = 1|do(M = 1 \& Y = 0)) = 0.8 > 0.00001 = P(E = 1|do(M = 0 \& Y = 0)) \quad (15)$$

$$P(E = 1|do(Y = 1 \& M = 0)) = 0.8 > 0.00001 = P(E = 1|do(Y = 0 \& M = 0)) \quad (16)$$

693 So we might consider whether we wish to modify **AC(M-R)** so that the setting of **W** isn't required to
 694 be the actual values of **W**.

695 But whether we wish to do so or not very much depends upon our attitude toward
 696 overdetermination (of probabilities). I'm inclined to agree with Lewis [23, pp. 207, 212] that it's
 697 intuitively doubtful that overdeterminers are causes. *Between them* the overdeterminers cause the
 698 outcome [23, pp. 207, 212], but I think it's doubtful that individually they are causes. In this vein
 699 Halpern [51, p. 3026] says: "Intuitively, ... they [the overdeterminers] are both parts of a cause, but not
 700 causes." The reason I think it's doubtful that individual overdeterminers are causes is precisely that, in
 701 the circumstances, they don't make a difference to whether or not (or with what probability) the effect
 702 occurs [cf. 51].³⁰

703 For those sympathetic to so called 'difference-making' approaches to actual causation (and note
 704 that SEM and PCM accounts of actual causation are among such approaches) there is the following
 705 reason for doubting that overdeterminers are causes. We all know that there are things that are
 706 plainly actual causes that don't straightforwardly make a difference to their effects (either by making
 707 a difference to whether-or-not they occur or by making a difference to the probability that they
 708 occur). Preemption cases show this.³¹ The intuition that motivates the de facto dependence/de
 709 facto probability-raising approach is that, nevertheless, a latent counterfactual dependence or
 710 probability-raising can be recovered by holding fixed certain features of the actual situation. But
 711 what would motivate analyzing actual causation in terms of a 'latent' probability-raising that is only
 712 present against a non-actual background. Why should the existence of difference-making holding fixed
 713 factors that are only present in a non-actual possible world indicate the existence of actual causation
 714 here in this world?

715 Can we afford not to take a stand on the present issue? That is, could we simply say that those
 716 who think each of a set of overdeterminers (of probabilities) is itself a cause should feel welcome to
 717 adopt an analysis of actual causation that weakens **AC(M-R)** by not requiring that the setting of **W**
 718 be to the actual values of **W**, while those of us who think that elements of a set of overdeterminers

³⁰ Sometimes overdeterminers might make a difference to the timing or manner in which an effect occurs. That is, they make a difference to whether or not (or the probability of whether) a certain 'alteration' [53] of the effect occurs. If so, they are not overdeterminers of the alteration. If we decide to identify the effect with the alteration (i.e. to take the effect to be modally fragile), then we just have a regular case where an effect has two causes (that are not overdeterminers) and our unmodified analysis will treat it as such. If we decide to identify the effect with the original, non-modally fragile effect, then there's genuine overdetermination (of probabilities). Unlike Lewis [53], I don't think that influencing which alteration of an event occurs is necessary or sufficient for causation of that event. For a demonstration of why it is not, see [54].

³¹ **Probabilistic Preemption** in fact shows that actual causes may *lower* the probability of their effects. But it can be modified into a case where the preempting cause makes no difference to the probability of its effect. For this to be the case, what we would need is for the negative relevance of my act to the explosion that comes by way of its negative relevance to your potential act to exactly balance (rather than 'overbalance') my act's tendency to promote the explosion because of the possibility that my U-232 will emit enough alpha particles that the Geiger counter reaches the threshold reading. This could be achieved by supposing that my act less strongly lowers the probability of your placing your radioactive material near to the Geiger counter than in the original example and/or supposing that your radioactive material is less potent than it is in the original example.

(of probabilities) are not actual causes should stick with the original version of **AC(M-R)**? (Perhaps different people just have slightly different concepts of actual causation.) In fact, weakening the requirement that the setting of **W** be to the actual values of **W** comes at a cost, as we shall see in Subsection 7.3 below. This cost is that there seem to be cases of clear non-causation where it is possible to reveal a ‘latent’ (and unneutralized) probability-raising by holding fixed certain variables at non-actual values.

Before showing this, it is worth noting that one modification to **AC(M-R)** and **AC(S)** is needed if these definitions are to capture the whole of the view of overdetermination cases that I have advocated. Specifically, while these definitions already capture the idea that individual overdeterminers aren’t actual causes, they don’t capture the view that, taken together, they are an actual cause. To capture this, we just need to modify the definitions by adopting a familiar feature of SEM approaches to actual causation (one possessed by the definitions given in 9, 17, and 51): namely, to allow that an actual cause might be a vector of values, rather than a single value. That is to say, in **AC(M-R)** and **AC(S)**, we would replace ‘ $X = x$ ’ with ‘ $\mathbf{X} = \mathbf{x}$ ’ and ‘ $X = x'$ ’ with ‘ $\mathbf{X} = \mathbf{x}'$ ’ throughout. In **AC(M-R)**, we’d replace ‘... there is a partition (\mathbf{Z}, \mathbf{W}) of $\mathcal{V} \setminus X, Y \dots$ ’ with ‘... there is a partition (\mathbf{Z}, \mathbf{W}) of $\mathcal{V} \setminus \mathbf{X}, \mathbf{Y} \dots$ ’.

Once we made this modification we would also need to introduce a ‘minimality’ condition into our analysis (as is also introduced in [9], [17], and [51]) in order to ensure that events that are intuitively not parts of causes don’t get counted as such. This would simply involve adding to **AC(M-R)** the requirement that there is no strict subset \mathbf{X}^C of \mathbf{X} such that, where $\mathbf{X}^C = \mathbf{x}^C$ denotes the variables in \mathbf{X}^C taking the values that they receive in the assignment $\mathbf{X} = \mathbf{x}$, and $\mathbf{X}^C = \mathbf{x}'^C$ denotes the variables in \mathbf{X}^C taking the values that they receive in the assignment $\mathbf{X} = \mathbf{x}'$, **AC(M-R)** (or rather the rest of it, once this condition is added) is satisfied when \mathbf{X} , $\mathbf{X} = \mathbf{x}$ and $\mathbf{X} = \mathbf{x}'$ are respectively replaced by \mathbf{X}^C , $\mathbf{X}^C = \mathbf{x}^C$, and $\mathbf{X}^C = \mathbf{x}'^C$ throughout.

This yields the desired result in the present case. To see this, consider the simple model $\mathcal{M}_{\text{Overdet}}$ generated from the variable set $\mathcal{V}_{\text{Overdet}} = \{M, Y, E\}$ and the veridical $do(\cdot)$ function for the world described in **Overdetermination of Probabilities**. Let $\mathbf{X} = \{M, Y\}$, so that $\mathbf{W}, \mathbf{Z} = \emptyset$ in the partition of $\mathcal{V}_{\text{Overdet}} \setminus \{M, Y\}, E$ and note that the variables in \mathbf{X} taking the values $M = 1 \& Y = 1$ rather than $M = 0 \& Y = 0$ raises the probability of $E = 1$ when we hold fixed the variables in \mathbf{W} (of which there are none) at their actual values. That is:

$$P(E = 1 | do(M = 1 \& Y = 1)) > P(E = 1 | do(M = 0 \& Y = 0)) \quad (17)$$

Thus the conjunctive event $M = 1 \& Y = 1$ de facto raises the probability of $E = 1$ relative to an alternative in which $M = 0 \& Y = 0$. Since $\mathbf{Z} = \emptyset$, this contingent probability-raising is automatically not neutralized. Note, moreover, that the minimality condition is satisfied, since neither $M = 1$ nor $Y = 1$ straightforwardly or de facto raises the probability of $E = 1$, as equalities 12, 13, and 14 indicate. (So neither $M = 1$ nor $Y = 1$ is alone an actual cause of $E = 1$ relative to $\mathcal{M}_{\text{Overdet}}$.) This means that **AC(M-R)** counts $M = 1 \& Y = 1$ rather than $M = 0 \& Y = 0$ as an actual cause of $E = 1$ relative to $\mathcal{M}_{\text{Overdet}}$.

The model $\mathcal{V}_{\text{Overdet}} = \{M, Y, E\}$ plainly satisfies (Partition), (Independence), and (Naturalness). It doesn’t represent any non-serious possibilities relative to the world described in **Overdetermination of Probabilities**, so it also satisfies (Serious Possibilities). Moreover, by assumption, the processes connecting your action and my action to the bomb’s exploding is complete (enough alpha particles from our U-232 chunks reach the detector). Consequently, a richer (in the sense of containing more variables) but otherwise appropriate model will not be one in which this de facto probability-raising is neutralized. Nor would any fine-graining of the variables involved eliminate this unneutralized de facto probability-raising. So (Stability) is also satisfied.

AC(S) therefore yields the verdict that $M = 1 \& Y = 1$ rather than $M = 0 \& Y = 0$ is an actual cause of $E = 1$, even though neither $M = 1$ nor $Y = 1$ is individually an actual cause of $E = 1$. This seems to me to be exactly the right result.

766 7.3. *Overlappings*

767 The following example, due to Schaffer [55, p. 41] (a similar example is given by Hitchcock [25, pp.
768 415-16]), further illustrates why we ought to be sceptical that ‘de facto’ probability-raising that is
769 revealed only by holding variables fixed at non-actual values should be taken to be indicative of actual
770 causation:

Overlapping

“An atom of U-238 and an atom of Ra-226 are placed in a box at t_0 (assume for simplicity that the box is otherwise empty). At t_1 the box contains an atom of Th-234, an alpha particle, and (still) an atom of Ra-226. The relevant physical laws are: (1) an atom of U-238 has a certain chance per unit interval of producing Th-234 and an alpha particle, (2) an atom of Ra-226 has a certain chance per unit interval of producing Rn-222 and an alpha particle, and (3) these chances are independent. ... And note that the Ra-226 aims to produce the alpha particle directly, since particle emissions from radioactive sources (as standardly understood) occur without hidden intermediaries”.

771 It’s clear, in this example, that the t_0 presence of the Ra-226 atom isn’t an actual cause of the t_1 presence
772 of the alpha particle, though the former straightforwardly raises the probability of the latter. The case
773 has a different structure to **Fizzling**, since there’s no intermediate process by which Ra-226 produces
774 alpha particles, and so no process to be incomplete or fizzled.

775 Still, this case can be handled by the present account, since the (continued) presence of the Ra-226
776 atom at t_1 is itself a neutralizer for the de facto probability-raising of the t_1 presence of the alpha
777 particle by the t_0 presence of the Ra-226 atom.

778 To see this, consider a model $\mathcal{M}_{\text{Overlap}}$ comprising a binary variable R_{t_0} that takes the value
779 $R_{t_0} = 1$ if the Ra-226 atom is present at t_0 and $R_{t_0} = 0$ otherwise, a binary variable R_{t_1} that takes the
780 value $R_{t_1} = 1$ if the Ra-226 atom is present at t_1 and $R_{t_1} = 0$ otherwise, a binary variable U_{t_0} that takes
781 the value $U_{t_0} = 1$ if the U-238 atom is present at t_0 and $U_{t_0} = 0$ otherwise, a binary variable U_{t_1} that
782 takes the value $U_{t_1} = 1$ if the U-238 atom is present at t_1 and $U_{t_1} = 0$ otherwise, a binary variable
783 A_{t_0} that takes the value $A_{t_0} = 1$ if there’s an alpha particle present at t_0 and $A_{t_0} = 0$ otherwise, and a
784 binary variable A_{t_1} that takes the value $A_{t_1} = 1$ if there’s an alpha particle present at t_1 and $A_{t_1} = 0$
785 otherwise. And suppose that the $do(\cdot)$ function associated with $\mathcal{M}_{\text{Overlap}}$ is the veridical one for the
786 world described by **Overlapping**.

787 Consider the partition of $\mathcal{V}_{\text{Overlap}} \setminus R_{t_0}, A_{t_1}$ such that $\mathbf{W} = \{A_{t_0}, U_{t_0}, U_{t_1}\}$ and $\mathbf{Z} = \{R_{t_1}\}$. Now, if
788 there were no chance either of the U-238 or of an alpha particle produced by the U-238 decay escaping
789 the box, then (since U-238 can only decay via the emission of an alpha particle) there’s not even de
790 facto probability-raising of $A_{t_1} = 1$ by $R_{t_0} = 1$ relative to this partition, since in that case:

$$P(A_{t_1} = 1 | do(R_{t_0} = 1 \& A_{t_0} = 0, U_{t_0} = 1 \& U_{t_1} = 0)) = 1 = P(A_{t_1} = 1 | do(R_{t_0} = 0 \& A_{t_0} = 0 \& U_{t_0} = 1 \& U_{t_1} = 0)) \quad (18)$$

791 That’s because, if the U-238 is in the box at t_0 but not at t_1 and if there’s zero chance of either the U-238
792 or an alpha particle escaping the box then the U-238 must have decayed and the alpha-particle must
793 be in the box.

794 But let’s suppose that there’s some chance of either the U-238 or an alpha particle that it produces
795 escaping the box between t_0 and t_1 . Then the t_1 presence of the Ra-226 raises the probability of there
796 being an alpha particle in the box at t_1 when the variables in \mathbf{W} are held fixed at their actual values,
797 $\{A_{t_0} = 0, U_{t_0} = 1, U_{t_1} = 0\}$. That is:

$$P(A_{t_1} = 1 | do(R_{t_0} = 1 \& A_{t_0} = 0 \& U_{t_0} = 1 \& U_{t_1} = 0)) > P(A_{t_1} = 1 | do(R_{t_0} = 0 \& A_{t_0} = 0 \& U_{t_0} = 1 \& U_{t_1} = 0)) \quad (19)$$

798 That is: the presence of the Ra-226 at t_0 raises the probability of the presence of an alpha-particle
 799 in the box at t_1 , even given the t_0 presence and t_1 absence of the U-238 (and the t_0 absence of an
 800 alpha particle), because there's some chance that the U-238 simply escapes the box or that an alpha
 801 particle that it produces does so and the t_0 presence of the Ra-226 raises the probability that there will
 802 nevertheless be an alpha particle present in the box at t_1 in such circumstances.

803 However, the de facto probability-raising of $A_{t_1} = 1$ by $R_{t_0} = 1$ is neutralized. That's because:

$$P(A_{t_1} = 1 | do(R_{t_0} = 1 \& R_{t_1} = 1 \& A_{t_0} = 0 \& U_{t_0} = 1, U_{t_1} = 0)) = P(A_{t_1} = 1 | do(R_{t_0} = 0 \& A_{t_0} = 0 \& U_{t_0} = 1, U_{t_1} = 0)) \quad (20)$$

804 That is, (in circumstances in which no alpha particle is present at t_0 and the U-238 atom is present at t_0
 805 but absent at t_1) the probability that an alpha particle is present at t_1 if the Ra-226 atom is present both
 806 at t_0 and t_1 is no higher than if the Ra-226 hadn't even been present at t_0 .

807 Of course, for **AC(M-R)** to count $R_{t_0} = 1$ as an actual cause of $A_{t_1} = 1$ relative to $\mathcal{M}_{\text{Overlap}}$ it
 808 need only be the case that there's *one* partition of $\mathcal{V}_{\text{Overlap}} \setminus R_{t_0}, A_{t_1}$ relative to which $R_{t_0} = 1$ bears the
 809 relation of non-neutralized de facto probability-raising to $A_{t_1} = 1$. But brief reflection makes it clear
 810 that this is not the case.

811 To see this, note that assigning A_{t_0}, U_{t_0} or U_{t_1} to **Z** rather than **W** while leaving R_{t_1} in **Z** won't
 812 help. No matter whether we hold fixed one, two, all, or none of A_{t_0}, U_{t_0} and U_{t_1} at their actual
 813 values, the probability of an alpha particle's being present at t_1 given that the Ra-226 was present
 814 at t_0 and at t_1 is no higher than if the Ra-226 had never been present in the first place. Thus the de
 815 facto probability-raising of $A_{t_1} = 1$ by $R_{t_0} = 1$ is neutralized for the subset $\{R_{t_1}\}$ of **Z**. Nor will
 816 assigning R_{t_1} to **W** rather than **Z** help (no matter what combination of $A_{t_0}, U_{t_0}, U_{t_1}$ or none is left in
 817 **W**). That's because the actual value $R_{t_1} = 1$ of R_{t_1} serves to 'screen off' the value of R_{t_0} from that of
 818 A_{t_1} so, if we include $R_{t_1} = 1$ as part of the fixed background $\mathbf{W} = \mathbf{w}^*$, then no relation of de facto
 819 probability-raising of $A_{t_1} = 1$ by $R_{t_0} = 1$ will be revealed. Consequently **AC(M-R)** doesn't count
 820 $R_{t_0} = 1$ as an actual cause of $A_{t_1} = 1$ relative to $\mathcal{M}_{\text{Overlap}}$.

821 Note that this case illustrates why it's important that we not allow non-actual settings of
 822 the variables in **W**. That's because if we let $\mathbf{W} = \{A_{t_0}, U_{t_0}, U_{t_1}, R_{t_1}\}$ and $\mathbf{Z} = \emptyset$, then 'de facto'
 823 probability-raising of $A_{t_1} = 1$ by $R_{t_0} = 1$ would be revealed by holding fixed the variables in **W**
 824 at the non-actual assignment $\{A_{t_0} = 0, U_{t_0} = 0, U_{t_1} = 0, R_{t_1} = 0\}$ or the non-actual assignment
 825 $\{A_{t_0} = 0, U_{t_0} = 1, U_{t_1} = 1, R_{t_1} = 0$. That is, in (non-actual) circumstances in which there's no alpha
 826 particle present at t_0 and in which the U-238 is present at both t_0 and t_1 or absent at both t_0 and t_1 and
 827 in which the Ra-226 is absent at t_1 , there's more chance of an alpha particle's being present at t_1 if the
 828 Ra-226 is present at t_0 . That's because the t_0 presence of the Ra-226 makes it more likely that the t_1
 829 absence of the Ra-226 is due to decay rather than the Ra-226 just having not being in the box in the
 830 first place. Note that, since $\mathbf{Z} = \emptyset$ in the partition of $\mathcal{V}_{\text{Overlap}}$ presently under consideration, this 'de
 831 facto' probability-raising is automatically not neutralized. So if **AC(M-R)** allowed non-actual settings
 832 of **W** to be considered, it would yield the result that $R_{t_0} = 1$ is an actual cause of $A_{t_1} = 1$ relative to
 833 $\mathcal{M}_{\text{Overlap}}$. Moreover, $\mathcal{M}_{\text{Overlap}}$ appears to be an appropriate model. (Naturalness), (Independence),
 834 (Partition), and (Serious Possibilities) all appear to be satisfied. By stipulation, (Veridicality) is satisfied
 835 relative to the world described in **Overlapping**. Finally, it's not at all obvious how $\mathcal{M}_{\text{Overlap}}$ could
 836 be expanded or refined into an appropriate model relative to which $R_{t_0} = 1$ doesn't 'de facto' raise
 837 the probability of $A_{t_1} = 1$, so it seems plausible that (Stability) is satisfied. So if **AC(M-R)** allowed
 838 non-actual settings of **W** to be considered, it appears that **AC(S)** would yield the erroneous result that
 839 $R_{t_0} = 1$ is an actual cause (simpliciter) of $A_{t_1} = 1$.

840 The disallowance of non-actual settings of \mathbf{W} is no *ad hoc* manoeuvre. Clearly the central reason
 841 that we identify the t_0 presence of the Ra-226 atom as *not* being an actual cause of the t_1 presence of the
 842 alpha particle is precisely that the Ra-226 atom is still present at t_1 . Considering what would have been
 843 the case had the Ra-226 atom not been present at t_1 seems clearly irrelevant and misleading regarding
 844 the causal status of the t_0 presence of the Ra-226 atom.

845 Because of its disallowance of non-actual settings of \mathbf{W} , **AC(M-R)** doesn't count $R_{t_0} = 1$ as an
 846 actual cause of $A_{t_1} = 1$ relative to $\mathcal{M}_{\text{Overlap}}$. Indeed, **AC(M-R)** doesn't count $R_{t_0} = 1$ as an actual
 847 cause of $A_{t_1} = 1$ relative to any otherwise appropriate model that includes R_{t_1} in its variable set. That's
 848 because, in the partition $\{\mathbf{W}, \mathbf{Z}\}$ of the model's variable set, either R_{t_1} will be included in \mathbf{W} in which
 849 case no de facto probability raising of $A_{t_1} = 1$ by $R_{t_0} = 1$ is revealed because the actual value of R_{t_1}
 850 screens off R_{t_0} from A_{t_1} , or R_{t_1} is included in \mathbf{Z} where its actual value serves to neutralize any de facto
 851 probability-raising of $A_{t_1} = 1$ by $R_{t_0} = 1$. This means that any otherwise appropriate model relative
 852 to which there's unneutralized de facto probability-raising of $A_{t_1} = 1$ by $R_{t_0} = 1$ can be expanded
 853 into one relative to which there isn't by means of the addition of R_{t_1} to its variable set, meaning
 854 that the original model violates (Stability). (What if the original model contains a variable that's
 855 logically or metaphysically related to R_{t_1} ? Well, if it satisfies (Naturalness), it seems that this could
 856 only be by containing a variable that's a fine-graining of R_{t_1} , since there doesn't seem to be any way of
 857 cross-cutting the states represented by the values of R_{t_1} while still representing reasonably natural
 858 states of affairs. On the other hand, a fine-graining of R_{t_1} might, for instance, represent the position and
 859 velocity of the Ra-226 atom if present. But the actual value of such a variable – which would represent
 860 the Ra-226 being present, perhaps at such-and-such a location in the box and with so-and-so a velocity
 861 – would itself screen off R_{t_0} from A_{t_1} and neutralize any de facto probability-raising of $A_{t_1} = 1$ by
 862 $R_{t_0} = 1$. So the latter wouldn't count as a cause of the former relative to such a model anyway.) The
 863 upshot is that **AC(S)** correctly discounts $R_{t_0} = 1$ as an actual cause of $A_{t_1} = 1$ in **Overlapping**.

864 The final point to note concerning **Overlapping** is that the definitions adopted here correctly
 865 count $U_{t_0} = 1$ as an actual cause of $A_{t_1} = 1$. To see this, consider the model $\mathcal{M}_{\text{Overlap}}$, described above
 866 and consider the partition of $\mathcal{V}_{\text{Overlap}} \setminus U_{t_0}, A_{t_1}$ such that $\mathbf{W} = \{A_{t_0}, R_{t_0}, R_{t_1}\}$ and $\mathbf{Z} = \{U_{t_1}\}$ and note
 867 that de facto probability-raising is revealed when we hold fixed the variables in \mathbf{W} at their actual
 868 values. That is:

$$P(A_{t_1} = 1 | do(U_{t_0} = 1 \& A_{t_0} = 0 \& R_{t_0} = 1 \& R_{t_1} = 1)) > P(A_{t_1} = 1 | do(U_{t_0} = 0 \& A_{t_0} = 0 \& R_{t_0} = 1 \& R_{t_1} = 1)) \quad (21)$$

869 That is, in the actual circumstances in which the Ra-226 atom is present both at t_0 and t_1 and there's
 870 no alpha particle present at t_0 , the probability of an alpha particle being present at t_1 is greater if the
 871 U-238 is present at t_0 than if it isn't.

872 Note that this de facto dependence isn't neutralized, because the following inequality also holds:

$$P(A_{t_1} = 1 | do(U_{t_0} = 1 \& U_{t_1} = 0 \& A_{t_0} = 0 \& R_{t_0} = 1 \& R_{t_1} = 1)) > P(A_{t_1} = 1 | do(U_{t_0} = 0 \& A_{t_0} = 0 \& R_{t_0} = 1 \& R_{t_1} = 1)) \quad (22)$$

873 That is, in the actual circumstances in which the Ra-226 atom is present both at t_0 and t_1 and there's
 874 no alpha particle present at t_0 , the probability of an alpha particle being present at t_1 is greater if the
 875 U-238 atom is present at t_0 and absent at t_1 than if it isn't even present at t_0 .

876 Definition **AC(M-R)** thus counts $U_{t_0} = 1$ as an actual cause of $A_{t_1} = 1$ relative to the model
 877 $\mathcal{M}_{\text{Overlap}}$. I've already noted that $\mathcal{M}_{\text{Overlap}}$ satisfies (Serious Possibilities), (Partition), (Independence),
 878 (Naturalness), and (Veridicality). Moreover, given that the actual value of U_{t_1} doesn't neutralize the de
 879 facto probability raising of $A_{t_1} = 1$ by $U_{t_0} = 1$ and given that, as Schaffer notes, U-238 decay doesn't
 880 occur via some intermediate process which could be incomplete, it doesn't seem that any variable or
 881 variables (representing reasonably natural states of affairs, etc.) could be added to $\mathcal{M}_{\text{Overlap}}$ that would
 882 neutralize this de facto probability-raising. (Nor does it seem that the existence of non-neutralized de

883 fact probability-raising in $\mathcal{M}_{\text{Overlap}}$ rests upon not representing the events involved in a fine-grained
 884 enough way.) Consequently, (Stabilty) is also satisfied. **AC(S)** therefore correctly counts the t_0 presence
 885 of the U-238 as an actual cause *simpliciter* of the t_1 presence of the alpha particle.

886 7.4. Bogus Preemption

887 The final example that we'll consider here is one given by Hitchcock [11, p. 519] that is an example we
 888 might call 'bogus preemption'. Hitchcock offers this as an example that causes problems for the SEM
 889 approaches to deterministic actual causation presented in [10], [8], and [9]. But it also arguably poses a
 890 problem for the analysis of actual causation introduced above:

Bogus Preemption

"Assistant Bodyguard puts a harmless antidote into Victim's coffee. Buddy then poisons the coffee, using a type of poison that is normally lethal, but which is countered by the antidote. Buddy would not have poisoned the coffee if Assistant had not administered the antidote first. Victim drinks the coffee and survives."

891 Hitchcock [11, p. 520] reports that "[m]any people, but by no means all, have the intuition that
 892 Assistant's adding the antidote to the coffee is not a cause of Victim's survival."

893 Suppose that we wish to accommodate this intuition.³² Then modification to **AC(M-R)** is needed.
 894 That's because the case is isomorphic to a preemption case. (Intuitively: just as my placing my U-232
 895 near to the Geiger counter preempts your placing your Th-228 near to the Geiger counter – a non-actual
 896 event – as an actual cause of the bomb's exploding in **Probabilistic Preemption**, so Assistant's putting
 897 the antidote into the coffee preempts Buddy's not putting the poison in – a non-actual event – as a
 898 cause of Victim's survival. Moreover, a variable representing the poison's undergoing the nullifying
 899 reaction with the antidote plays a role analogous to the Geiger counter's reaching the threshold reading
 900 in **Probabilistic Preemption**.) The fact that the case is isomorphic to a preemption case means that the
 901 analysis given here, just like the SEM analyses of deterministic actual causation given in [10], [8], and
 902 [9], treats Assistant's action as an actual cause of Victim's survival.³³

903 To see the trouble posed for the present analysis more clearly, consider a model $\mathcal{M}_{\text{BogusPre}}$ with
 904 a variable set $\mathcal{V}_{\text{BogusPre}}$ comprising the binary variables A , which takes the value $A = 1$ if Assistant
 905 puts the antidote in the coffee, and $A = 0$ otherwise; P , which takes the value $P = 1$ if Buddy puts the
 906 poison in the coffee, and $P = 0$ otherwise; N , which takes the value $N = 1$ if the poison undergoes
 907 the nullifying reaction with the antidote, and $N = 0$ otherwise; and S which takes the value $S = 1$ if
 908 Victim survives, and $S = 0$ otherwise. And suppose that the $do(\cdot)$ function associated with $\mathcal{M}_{\text{BogusPre}}$
 909 is the veridical one relative to the world described in **Bogus Preemption**.

910 Now suppose that we evaluate the claim that $A = 1$ is an actual cause of $S = 1$ relative to
 911 $\mathcal{M}_{\text{BogusPre}}$. Consider the partition of $\mathcal{V}_{\text{BogusPre}} \setminus A, S$ such that $\mathbf{W} = \{P\}$ and $\mathbf{Z} = \{N\}$. And note that
 912 holding the variable in \mathbf{W} fixed at its actual value, $P = 1$, reveals de facto probability-raising of $S = 1$
 913 by $A = 1$:

³² I'm not convinced that the payoff of doing so is worth the costs associated with the standard approach to accommodating this intuition that is taken within the SEM literature on deterministic actual causation. (And I don't have any novel approach of my own to propose.) Blanchard and Schaffer [49] describe these costs. The apparent equivocality of intuition about the case suggests that the payoff is not so great after all. Still, in what follows, I shall show that the present account is (once appropriately tweaked) as well-placed as its deterministic cousins to accommodate an intuition that Assistant's act was not an actual cause.

³³ In fact, Halpern and Pearl [9, Section 5] suggest a refinement of their analysis, which is roughly along the lines of that discussed below, which may allow them to avoid this result.

$$P(S = 1|do(A = 1 \& P = 1)) > P(S = 1|do(A = 0 \& P = 1)) \quad (23)$$

914 That is, holding fixed that Buddy puts poison in the coffee, the probability of Victim surviving is higher
 915 if Assistant has put the antidote in than if she hasn't. Moreover, this de facto probability-raising is not
 916 neutralized, because:

$$P(S = 1|do(A = 1 \& N = 1 \& P = 1)) > P(S = 1|do(A = 0 \& P = 1)) \quad (24)$$

917 That is, holding fixed that Buddy puts poison in the coffee, the probability of Victim surviving is higher
 918 if Assistant puts the antidote in and the antidote nullifies the poison than if Assistant had never put
 919 the antidote into the coffee in the first place.

920 So **AC(M-R)** counts $A = 1$ as an actual cause of $S = 1$ relative to $\mathcal{M}_{\text{BogusPre}}$. $\mathcal{M}_{\text{BogusPre}}$ satisfies
 921 (Partition), (Independence), and (Naturalness). By stipulation, it also satisfies (Veridicality) for
 922 the scenario in question. It doesn't seem that there's any unmodelled neutralizer of the de facto
 923 probability-raising of $S = 1$ by $A = 1$ (nor does it seem that any fine-graining of the variables involved
 924 will reveal this de facto probability-raising to be spurious, as in the case of **Determinable Effect**), so
 925 it seems that $\mathcal{M}_{\text{BogusPre}}$ satisfies (Stability). On the assumption that it satisfies (Serious Possibilities)
 926 (more on this in a moment), **AC(S)** counts $A = 1$ as an actual cause *simpliciter* of $S = 1$, which, to some
 927 at least, seems an implausible result.

928 Once it was noticed that the SEM analyses of deterministic actual causation given by Hitchcock
 929 [10] and Halpern and Pearl [8] also yield this result, advocates of the SEM approach attempted to
 930 deal with it by putting restrictions on what values other variables in a model could be held fixed at
 931 evaluating whether the value of one variable is an actual cause of another.³⁴ In terms of the approach
 932 pursued here, the idea would be to say that unneutralized de facto probability-raising revealed by
 933 holding fixed the elements of \mathbf{W} at their actual values $\mathbf{W} = \mathbf{w}^*$ is only indicative of actual causation if a
 934 certain further condition is satisfied. The idea would be to rule that, for the partition of $\mathcal{V}_{\text{BogusPre}} \setminus A, S$
 935 such that $\mathbf{W} = \{P\}$ and $\mathbf{Z} = \{N\}$, this further condition is not satisfied for the actual value, $P = 1$, of
 936 the variable in \mathbf{W} .

937 An idea developed by, among others, Halpern ([14], [57]) and Halpern and Hitchcock [16] is that
 938 this further condition can be framed in terms of considerations of *normality*. Applied to the present
 939 definitions, the idea is, when assessing whether $X = x$ rather than $X = x'$ is an actual cause of $Y = y$,
 940 (unneutralized) de facto dependence revealed by holding fixed the variables \mathbf{W} at their actual values
 941 $\mathbf{W} = \mathbf{w}^*$ is indicative of actual causation iff the most normal world in which $X = x'$ and $\mathbf{W} = \mathbf{w}^*$
 942 holds – the 'witness' world – is at least as normal as the actual world.³⁵ More specifically, the modified
 943 **AC(M-R)** would go as follows:

³⁴ Another case that has been used to motivate this sort of modification is identified by Hiddleston [56, p. 32] and dubbed 'bogus prevention' by Hitchcock [11, p. 523]. This is isomorphic to overdetermination cases, but only poses a problem to accounts that treat overdeterminers as causes, which the present account does not.

³⁵ Halpern and Hitchcock [17] adopt a more radical approach: they take actual causation to be gradable, with the degree of normality of the witness world determining the degree to which $X = x$ is an actual cause of $Y = y$ (when $Y = y$ counterfactually depends upon $X = x$ holding suitable factors fixed). The notion that actual causation might be gradable is a complication that I shall not explore here, though I don't see any reason to think that the proposal that the degree of normality of the witness determines the degree of actual causation wouldn't transfer smoothly to the present analysis.

AC(M-R)'

Where $x, x' \in \mathcal{R}(X)$ and $y \in \mathcal{R}(Y)$, $X = x$ rather than $X = x'$ is an actual cause of $Y = y$ relative to a model $\mathcal{M} = \langle \mathcal{V}, \mathcal{R}, \mathcal{C}, \Omega, \mathcal{F}, do(\cdot) \rangle$ (with $X, Y \in \mathcal{V}$) in world θ iff there is a partition (\mathbf{Z}, \mathbf{W}) of $\mathcal{V} \setminus X, Y$ such that, where $\mathbf{W} = \mathbf{w}^*$ are the actual values the variables in \mathbf{W} take in θ , the witness to $X = x' \& \mathbf{W} = \mathbf{w}^*$ is at least as normal as θ , and for all subsets \mathbf{Z}' of \mathbf{Z} (where $\mathbf{Z}' = \mathbf{z}^*$ are the actual values that the variables in \mathbf{Z}' take in θ):

$$(IN) P(Y = y | do(X = x \& \mathbf{W} = \mathbf{w}^* \& \mathbf{Z}' = \mathbf{z}^*)) > P(Y = y | do(X = x' \& \mathbf{W} = \mathbf{w}^*))$$

944 Halpern and Hitchcock suggest that various sorts of normality feed into determining the overall
 945 normality of a world, including statistical normality, default behaviors, moral and social norms, and
 946 norms of proper functioning.

947 As applied to the present example, the idea would be that a world in which Assistant doesn't
 948 put the antidote into Victim's coffee but Buddy nevertheless puts the poison in is an abnormal one,
 949 and more abnormal than the actual world in which Assistant puts the antidote in and Buddy puts
 950 the poison in. This might be justified on the grounds that Buddy's putting the poison in despite
 951 Assistant's not putting the antidote in would be a violation of a moral norm (or at least more of a
 952 violation of a moral norm than her putting the poison in when Assistant had already put the antidote
 953 in). Consequently, the fact that de facto probability-raising of $S = 1$ by $A = 1$ is revealed when it is
 954 held fixed that $P = 1$ is not indicative of $A = 1$ being an actual cause of $S = 1$.

955 In order for this proposal to work it would have to preserve the desirable results that we get in
 956 other cases. Thus in **Probabilistic Preemption**, for instance, it would be important that the de facto
 957 probability-raising of the explosion by my placing my U-232 near to the Geiger counter that is revealed
 958 by holding fixed your non-placement of your Th-228 near to the Geiger counter still be counted as
 959 genuinely indicative of actual causation. To get this result it would be necessary that, according to
 960 the appropriate notion of normality, a world in which you don't place your Th-228 near to the Geiger
 961 counter and I don't place my U-232 near to the Geiger counter either is at least as normal as the actual
 962 world, in which I place my U-232 but you don't place your Th-228 near to the Geiger counter. But this
 963 is so on quite a reasonable sense of normality: after all, your placing your Th-228 near to the Geiger
 964 counter violates moral norms (given the setup involving the bomb) and also, simply in virtue of being
 965 a positive action rather than an inaction, is a non-default behavior.

966 Two obvious questions present themselves at this point. First, does this appeal to 'normality'
 967 do any work that the appeal to 'serious possibilities' (in defining model appropriateness) does not
 968 already do? Second, if it does, can we drop the appeal to serious possibilities in favour of this appeal
 969 to normality? I'd give a cautious affirmative answer to each of these questions (cautious because this
 970 partly depends upon how the account of 'normality' is worked out and what counts as a 'serious
 971 possibility').

972 Regarding the first question, one might ask, for instance, whether $\mathcal{M}_{\text{BogusPre}}$ violates (Serious
 973 Possibilities) so that we can conclude that the unneutralized de facto probability-raising of $S = 1$
 974 by $A = 1$ in this model fails to be indicative of actual causation. If so, we wouldn't need to appeal
 975 to the normality of the witness world to secure the latter result. Perhaps, for instance, we could
 976 argue that a model including both A and P is inappropriate model because such a model allows the
 977 representation of a non-serious possibility: namely, the possibility that Buddy poisons the coffee even
 978 though Assistant hasn't put the antidote in.

979 But I don't think that this strategy of trying to secure the desired result by simply appealing to
 980 (Serious Possibilities) will work. (Serious Possibilities) was never intended by its advocates to rule as
 981 inappropriate models that include only variables that represent salient parts of the causal structure
 982 being modelled, as both S and A do for **Bogus Preemption**. Rather, it was introduced to rule as
 983 inappropriate models including variables representing highly non-salient factors, such as whether or

984 not McCartney intercepted the bullets in the case of the JFK assassination. Indeed, interpreting (Serious
 985 Possibilities) as ruling out models including the former sort of variable and not just those including the
 986 latter sort would fatally undermine treatments of actual causation that appeal to SEMs or PCMs. That's
 987 because even models that seem like perfectly reasonable representations of just the salient events in
 988 causal scenarios are typically such that there is *some* assignment of values to the variables they include
 989 that corresponds to a rather remote possibility.

990 Consider, for instance, M_{ProbPre} . And note that there seems to be no reason why we should
 991 suppose that your commitment to not place your Th-228 near to the Geiger counter if I place my
 992 U-232 near to the Geiger counter in **Probabilistic Preemption** should be any weaker than Buddy's
 993 commitment not to poison the coffee if Assistant doesn't put the antidote in in **Bogus Preemption**. But,
 994 by including M and Y in M_{ProbPre} , we allow the representation of the possibility that I place my U-232
 995 near the Geiger counter *and* you place your Th-228 near to the Geiger counter. Ruling such a model
 996 to be non-apt because it violates (Serious Possibilities) would be highly problematic, since it's only
 997 by including both M and Y that we can represent the de facto probability-raising of $E = 1$ by $M = 1$
 998 that is indicative of actual causation in this case. As we've seen, interpreting (Serious Possibilities) so
 999 that it doesn't rule out a model including M and Y , but introducing a 'naturalness' restriction on what
 1000 settings of W are such that unneutralized de facto dependence relative to them is indicative of actual
 1001 causation plausibly preserves the correct result in this case.

1002 On the other hand, once the appeal to naturalness has been invoked, it's plausible that we can
 1003 dispense with (Serious Possibilities). If we do so, a model of the JFK assassination counts as appropriate
 1004 even if it includes a variable corresponding to whether or not McCartney got in the way of the bullets.
 1005 Still, the appeal to naturalness plausibly rules out McCartney's failure to intercept the bullets from
 1006 counting as an actual cause of JFK's death because a world in which McCartney intercepts them would
 1007 presumably be an abnormal one by any reasonable standards.

1008 8. Conclusion

1009 In this paper, PCMs have been drawn upon in providing an analysis of actual causation. The aspiration
 1010 has been to provide a treatment of probabilistic actual causation that matches the sophistication and
 1011 success of those treatments of deterministic actual causation that draw upon SEMs, whilst also paying
 1012 due attention to the unique challenges that arise in the probabilistic case. It has been shown that this
 1013 analysis gives the correct treatment of a range of test cases, some of which have been raised in the
 1014 literature as posing problems for traditional accounts of probabilistic actual causation, and some of
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 1016 discussed in the deterministic actual causation literature.

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1023

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